# METHOD 516.6 SHOCK

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## **METHOD 516.6**

## SHOCK

NOTE: Tailoring is essential. Select methods, procedures, and parameter levels based on the tailoring process described in Part One, paragraph 4.2.2, and Annex C. Apply the general guidelines for laboratory test methods described in Part One, paragraph 5 of this standard.

## 1. SCOPE.

## 1.1 Purpose.

Shock tests are performed to:

- a. provide a degree of confidence that materiel can physically and functionally withstand the relatively infrequent, non-repetitive shocks encountered in handling, transportation, and service environments. This may include an assessment of the overall materiel system integrity for safety purposes in any one or all of the handling, transportation, and service environments;
- b. determine the materiel's fragility level, in order that packaging may be designed to protect the materiel's physical and functional integrity; and
- c. test the strength of devices that attach materiel to platforms that can crash.

## **1.2** Application.

Use this method to evaluate the physical and functional performance of materiel likely to be exposed to mechanically induced shocks in its lifetime. Such mechanical shock environments are generally limited to a frequency range not to exceed 10,000 Hz, and a time duration of not more than 1.0 second. (In most cases of mechanical shock the significant materiel response frequencies will not exceed 4,000 Hz and the duration of materiel response will not exceed 0.1 second.) The materiel response to the mechanical shock environment will, in general, be highly oscillatory, of short duration, and have a substantial initial rise time with large positive and negative peak amplitudes of about the same order of magnitude.<sup>1</sup> The peak responses of materiel to mechanical shock will, in general, be enveloped by a decreasing form of exponential function in time. In general, mechanical shock applied to a complex multi-modal materiel system will cause the materiel to respond to (1) forced frequencies imposed on the materiel from the external excitation environment, and (2) the materiel's resonant natural frequencies either during or after application of the excitation. Such response may cause:

- a. materiel failure as a result of increased or decreased friction between parts, or general interference between parts;
- b. changes in materiel dielectric strength, loss of insulation resistance, variations in magnetic and electrostatic field strength;
- c. materiel electronic circuit card malfunction, electronic circuit card damage, and electronic connector failure. (On occasion, circuit card contaminants having the potential to cause short circuit may be dislodged under materiel response to shock.);
- d. permanent mechanical deformation of the materiel as a result of overstress of materiel structural and non-structural members;
- e. collapse of mechanical elements of the materiel as a result of the ultimate strength of the component being exceeded;
- f. accelerated fatiguing of materials (low cycle fatigue);
- g. potential piezoelectric activity of materials, and
- h. materiel failure as a result of cracks in fracturing crystals, ceramics, epoxies, or glass envelopes.

<sup>&</sup>lt;sup>1</sup> For high impact velocity shock, e.g., penetration shocks, there may be significantly less or no oscillatory behavior with substantial area under the acceleration response curve.

## 1.3 Limitations.

This method does not include:

- a. The effects of shock experienced by materiel as a result of pyrotechnic device initiation. For this type of shock see Method 517.1, Pyroshock.
- b. The effects experienced by materiel to very high level localized impact shocks, e.g., ballistic impacts. For this type of shock, devise specialized tests based on experimental data, and consult Method 522.1, Ballistic Shock.
- c. The high impact shock effects experienced by materiel aboard a ship due to wartime service (from nuclear or conventional weapons). Consider performing shock tests for shipboard materiel in accordance with MIL-S-901 (paragraph 6.1, reference c).
- d. The effects experienced by fuse systems. Perform shock tests for safety and operation of fuses and fuse components in accordance with MIL-STD-331 (paragraph 6.1, reference d).
- e. The effects experienced by materiel that is subject to high pressure wave impact, e.g., pressure impact on a materiel surface as a result of firing of a gun. For this type of shock and subsequent materiel response, devise specialized tests based on experimental data and consult Method 519.6, Gunfire Shock.
- f. The shock effects experienced by very large extended materiel, e.g., building pipe distribution systems, over which varied parts of the materiel may experience different and unrelated shock events. For this type of shock, devise specialized tests based on experimental data.
- g. Special provisions for performing shock tests at high or low temperatures. Perform tests at room ambient temperature unless otherwise specified. Guidelines found in this section of the standard, however, may be helpful in setting up and performing shock tests at high or low temperatures.
- h. Testing of materiel worn on or attached to humans.
- i. Time Waveform Replication (TWR) methodology. The specifics of TWR are defined in Methods 525 and 527.

## 2. TAILORING GUIDANCE.

## 2.1 Selecting the Shock Method.

After examining requirements documents and applying the tailoring process in Part One of this standard to determine where mechanical shock environments are foreseen in the life cycle of the materiel, use the following to confirm the need for this method and to place it in sequence with other methods.

## 2.1.1 Effects of shock.

Mechanical shock has the potential for producing adverse effects on the physical and functional integrity of all materiel. In general, the level is affected by both the magnitude and the duration of the shock environment. Durations of shock that correspond with natural frequency periods of the materiel and/or periods of major frequency components in input shock environment waveforms that correspond with natural frequency periods of the materiel will magnify the adverse effects on the materiel's overall physical and functional integrity.

## 2.1.2 Sequence among other methods.

- a. <u>General.</u> See Part One, paragraph 5.5.
- b. <u>Unique to this method</u>. Sequencing among other methods will depend upon the type of testing, i.e., developmental, qualification, endurance, etc., and the general availability of test items for test. Normally, schedule shock tests early in the test sequence, but after any vibration tests.
  - If the shock environment is deemed particularly severe, and the chances of materiel survival without major structural or operational failure are small, the shock test should be first in the test sequence. This provides the opportunity to redesign the materiel to meet the shock requirement before testing to the more benign environments.
  - (2) If the shock environment is deemed severe, but the chance of the materiel survival without structural or functional failure is good, perform the shock test after vibration and thermal tests, allowing the stressing of the test item prior to shock testing to uncover combined vibration, and temperature failures.
  - (3) There are often advantages to applying shock tests before climatic tests, provided this sequence represents realistic service conditions. Test experience has shown that climate-sensitive defects

often show up more clearly after the application of shock environments. However, internal or external thermal stresses may permanently weaken materiel resistance to vibration and shock that may go undetected if shock tests are applied before climatic tests.

## 2.2 Selecting a Procedure.

This method includes eight test procedures.

- a. Procedure I Functional Shock.
  - b. Procedure II Materiel to be packaged.
  - c. Procedure III Fragility.
  - d. Procedure IV Transit Drop.
  - e. Procedure V Crash Hazard Shock Test.
  - f. Procedure VI Bench Handling.
- g. Procedure VII Pendulum Impact.
  - h. Procedure VIII Catapult Launch/Arrested Landing.

## 2.2.1 Procedure selection considerations.

Based on the test data requirements, determine which test procedure, combination of procedures, or sequence of procedures is applicable. In many cases, one or more of the procedures will apply. Consider all shock environments anticipated for the materiel during its life cycle, both in its logistic and operational modes. When selecting procedures, consider:

- a. <u>The operational purpose of the materiel</u>. From requirement documents, determine the operations or functions to be performed by the materiel before, during and after the shock environment.
- b. <u>The natural exposure circumstances</u>. Procedures I through VII specify single shocks that result from momentum exchange between materiel or materiel support structures and another body. Procedure VIII (catapult launch) contains a sequence of two shocks separated by a comparatively short duration vibration, i.e., transient vibration. Procedure VIII (Catapult Launch/Arrested Landing) may be considered a single shock followed by a transient vibration.
- c. <u>Data required</u>. The test data required to document the test environment and to verify the performance of the materiel before, during, and after test.
- d. <u>Procedure sequence</u>. Refer to paragraph 2.1.2.

## 2.2.2 Difference among procedures.

- a. <u>Procedure I Functional Shock</u>. Procedure I is intended to test materiel (including mechanical, electrical, hydraulic, and electronic) in its functional mode and to assess the physical integrity, continuity and functionality of the materiel to shock. In general, the materiel is required to function during the shock and to survive without damage to shocks representative of those that may be encountered during operational service.
- b. <u>Procedure II Materiel to be Packaged</u>. Procedure II is to be used when materiel will require a shipping container. It specifies a minimum critical shock resistance level to a handling drop height. The shock definition may be furnished to a package designer as a design criterion. This procedure is not intended for the test of extremely fragile materiel, e.g., missile guidance systems, precision-aligned test equipment, gyros, inertial guidance platforms, etc. For extremely fragile materiel where quantification of shock resistance is required, consider Procedure III. See paragraph 2.3 below for processing techniques useful in expressing shock resistance criteria.
- c. <u>Procedure III Fragility</u>. Procedure III is used to determine a materiel's ruggedness or fragility so that packaging can be designed for the materiel, or so the materiel can be redesigned to meet transportation and/or handling requirements. This procedure is used to determine the critical shock conditions at which there is reasonable chance of structural and/or functional system degradation. To achieve the most realistic criteria, perform the procedure at environmental temperature extremes. See paragraph 2.3 below for processing techniques useful in expressing shock fragility criteria.
- d. <u>Procedure IV Transit Drop</u>. Procedure IV is intended for materiel either outside of or within its transit or combination case, or as prepared for field use (carried to a combat situation by man, truck, rail, etc.).

This procedure is used to determine if the materiel is capable of withstanding the shocks normally induced by loading and unloading when it is (1) outside of its transit or combination case, e.g., during routine maintenance, when being removed from a rack, being placed in its transit case, etc., or (2) inside its transit or combination case. Such shocks are accidental, but may impair the functioning of the materiel. This procedure is not intended for shocks encountered in a normal logistic environment as experienced by materiel inside shipping containers (see Procedure II (Materiel to be Packaged) and Procedure VII (Pendulum Impact).

- e. <u>Procedure V Crash Hazard Shock Test</u>. Procedure V is for materiel mounted in air or ground vehicles that could break loose from its mounts, tiedowns or containment configuration during a crash and present a hazard to vehicle occupants and bystanders. This procedure is intended to verify the structural integrity of materiel mounts, tiedowns or containment configuration during simulated crash conditions. Use the test to verify the overall structural integrity of the materiel, i.e., parts of the materiel are not ejected under the shock. This procedure is not intended for materiel transported as cargo for which Method 513.6, Acceleration, or Method 514.6, Vibration, could be applied. The crash hazard can be evaluated by a static acceleration test (Method 513 Procedure III) and/or a transient shock (Method 516 Procedure V). The requirement for one or both procedures must be evaluated based on the test item.
- f. Procedure VI Bench Handling. Procedure VI is intended for materiel that may typically experience bench handling, bench maintenance, or packaging. It is used to determine the ability of the materiel to withstand representative levels of shock encountered during typical bench handling, bench maintenance, or packaging. Such shocks might occur during materiel repair. This procedure may include testing for materiel with protrusions that may be easily damaged without regard to gross shock on the total materiel. The nature of such testing is highly specialized and must be performed on a case-by-case basis, noting the configuration of the materiel protrusions and the case scenarios for damage during such activities as bench handling, maintenance, and packaging. This procedure is appropriate for medium-to-large test materiel out of its transit or combination case that has a maximum dimension greater than approximately 23 cm (9 inches). Small materiel systems, in general, will be tested to higher levels during Procedure IV, Transit Drop.
- g. <u>Procedure VII Pendulum Impact</u>. Procedure VII is intended to test the ability of large shipping containers to resist horizontal impacts, and to determine the ability of the packaging and packing methods to provide protection to the contents when the container is impacted. This test is meant to simulate accidental handling impacts, and is used only on containers that are susceptible to accidental end impacts. The pendulum impact test is designed specifically for large and/or heavy shipping containers that are likely to be handled mechanically rather than manually.

NOTE: The rail impact test, formerly Procedure VII, has been moved to Method 526.

h. <u>Procedure VIII - Catapult Launch/Arrested Landing</u>. Procedure VIII is intended for materiel mounted in or on fixed-wing aircraft that are subject to catapult launches and arrested landings. For catapult launch, materiel may experience a combination of initial shock followed by a low level transient vibration of some duration having frequency components in the neighborhood of the mounting platform's lowest frequencies, and concluded by a final shock according to the catapult event sequence. For arrested landing, materiel may experience an initial shock followed by a low level transient vibration of some duration having frequency components in the neighborhood of the mounting platform's lowest frequencies.

## 2.3 Determine Test Levels and Conditions.

Having selected this method and relevant procedures (based on the materiel's requirements documents and the tailoring process), complete the tailoring process by identifying appropriate parameter levels, applicable test conditions, and test techniques for the selected procedures. Base these selections on the requirements documents, the Life Cycle Environmental Profile (LCEP), and information provided with this procedure. Consider the following when selecting test levels:

## 2.3.1 General considerations – Terminology and illustration for complex transient.

## 2.3.1.1 Shock.

Shock is the term applied to a comparatively short time (usually much less than the period of the *fundamental* frequency of the materiel) and moderately high level (above even extreme vibration levels) force impulse applied as an input to the material. Generally the force impulse input is distributed to the materiel (over the materiel surface or into the materiel body) and difficult if not impossible to measure directly in terms of force magnitude. Materiel response acceleration will generally be the variable for measurement and used in characterization of the effects of the shock. This does not preclude other variables of materiel response such as velocity, displacement, strain, force or pressure from being used and processed in an analogous manner, as long as the interpretation of the measurement variable is clear and the measurement instrumentation configuration is validated, e.g., measurements made within the significant frequency range of materiel response, etc. Figure 516.6-1 displays a moderately complex measured materiel response acceleration that represents a materiel shock time history. Figure 516.6-2 is the velocity determined from integrating the shock after the shock has been high pass filtered at 5 Hz to remove the DC component. The response acceleration time history can be characterized in several ways. The observed time history duration and amplitude provide one characterization. Section 2.3.1.1.a will discuss in more detail duration characterization and peak time history amplitudes above an instrumentation noise floor, useful for preliminary shock identification. Analysis of the time history as a digital sequence can be performed using the Shock Response Spectra (SRS), Energy Spectral Density (ESD), Fourier Spectra (FS), Time Domain Moments (TDM) or Energy Methods (EM). All these forms of analyses serve to provide additional unique characterizations. The SRS and the ESD will be discussed and illustrated below. TDM and EM represent new developments that show promise for shock characterization



Figure 516.6-1. Sample shock response acceleration time history (5 Hz to 6000 Hz).

a. In MIL-STD-810E Method 516.5,  $T_E$  is defined to be the minimum length of time that contains all time history magnitudes exceeding in absolute value one-third of the shock peak magnitude absolute value,  $A_p$ ; i.e.,  $1/3 A_p$ , associated with the shock. This definition is generally adequate for SRS and ESD processing but fails to fully characterize the shock in that it may lead to truncation of important shock information well above the instrumentation noise floor. For example, truncation of important shock information may result if the shock (1) asymmetrically reaches its peak value slowly or (2) has a significant noise spike that is not removed prior to either the beginning or end of the shock. The measurement system noise floor prior to the shock usually provides the shock initial point. Theoretically this is defined as the "last point" consistent with the level of the measurement system noise floor. This initial shock point can usually be determined easily based upon time history inspection by a trained analyst. For identification of a terminal point of a shock, generally a shock will not decay to the measurement system noise floor until long after the significant information in the shock has ceased. A  $1/3 A_p$  truncation criteria is unreliable and will generally truncate the shock before significant shock information

ceases. An additional definition for effective shock duration denoted  $T_e$ , may be stated as follows:

The effective shock duration,  $T_e$  is the <u>minimum</u> length of continuous time that contains the root-mean-square (RMS) time history amplitudes exceeding in value ten percent of the peak RMS amplitude associated with the shock event. The averaging time for the unweighted RMS computation is assumed to be between ten and twenty percent of  $T_e$ .

The RMS averaging time (time over which unweighted mean-square time history amplitudes are averaged) nonuniformly biases the shock time history root-mean-square information since the bias error is a function of the "shape" of the true root-mean-square of the time history. However, the root-mean-square estimate as a function of averaging time does provide a crude visual indicator of the location of the "energy content" of the time history. It is often advantageous to compare results from two or three averaging times for selection  $T_e$ . It may be necessary for a trained analyst to define *the shock* or *shocks* in cases in which RMS amplitudes temporarily go below the ten percent peak RMS amplitude criteria and decide if only one shock is present or whether multiple shocks are present. This decision should be based upon phenomenological considerations related to the nature of the physical cause of the shock. For multiple shocks it is possible to accurately replicate the measured environment utilizing Time Waveform Replication in Method 525 or Method 527.

The above definition for  $T_e$  is complex in that generally, for a given shock, it may require an iterative procedure to establish  $T_e$ . However, the judgment of an experienced measurement shock analyst will often be satisfactory in determining an effective duration,  $T_e$ , consistent with the above definition without rigorously applying the analytical definition. For determination of the effective shock duration,  $T_e$ , involved in the processing of a measured transient time history it is important that (a) information inherent in the complex transient is preserved and (b) information related to the measurement instrumentation noise is minimized.

For a *simple form* of shock time history having a window that has basically a polynomial ramp up followed by an exponential ramp down, Annex B provides a stochastic based empirical relationship between  $T_e$  and  $T_E$ . The results of Annex B would seem to indicate that generally for this simple form of shock time history,  $T_E$ , may severely underestimate the shock duration if the above definitions of  $T_E$  and  $T_e$  are strictly adhered to. Annex B provides a simple empirically derived factor for converting from  $T_E$  to  $T_e$  in the older tables.

Figure 516.6-3 illustrates the effective shock durations  $T_E$  and  $T_e$  on a truncated form of the shock time history depicted in Figure 516.6-1. Because of the extended nature of the shock,  $T_E$  and  $T_e$  are substantially different.

Figure 516.6-4 provides an estimate of the short time average RMS of the time history in Figure 516.6-1 along with  $T_E$ ,  $T_e$  and  $0.1A_{RMS}$ . On Figure 516.6-4, the short time averaging time used to compute the RMS level is displayed at ten and twenty percent of  $T_e$ .



Figure 516.6-2. Corresponding shock response velocity time history.



Figure 516.6-3 Shock response time history displaying effective durations  $T_{\rm E}$  and  $T_{\rm e}$ .

Shock Response Spectrum (SRS): The SRS value at a given undamped natural oscillator frequency, b.  $f_{n,b}$  describes the maximum response of the mass of a damped single degree of freedom system (SDOF) at this frequency to a shock base input time history of duration T<sub>e</sub>. Damping of the SDOF is expressed in terms of a "Q" (quality factor) value where a Q of 50 represents 1 percent critical damping; a Q of 10, 5 percent critical damping; and a Q of 5, 10 percent critical damping of the SDOF. For processing of shock response data, the absolute acceleration maximax SRS has become primary analysis descriptor. In this measurement description of the shock, the maximax acceleration values are plotted on the ordinate with the undamped natural frequency of the SDOF with base input plotted along the abscissa. The frequency range over which the SRS is computed extends from a lowest frequency of interest up to a frequency at which the flat portion of the spectrum has been reached. This latter upper frequency requirement helps ensure no high frequency content in the spectrum is neglected. The lowest frequency of interest is determined by the frequency response characteristics of the materiel under test. For fmin, the lowest frequency of interest, (defined as at least one octave below the first natural mode frequency ( $f_{min}$ ) of the test item) the SRS is computed over a time interval T<sub>e</sub> or  $1/2f_{min}$ , (whichever is the greatest) starting with the first amplitude rise of the shock. A more complete description of the shock (potentially more useful for shock damage assessment, but not widely accepted) can be obtained by determining the maximax pseudo-velocity response spectrum and plotting this on four-coordinate paper where, in pairs of orthogonal axes, the maximax pseudo-velocity response spectrum is represented by the ordinate, with the undamped natural frequency being the abscissa and the maximax absolute acceleration along with maximax pseudo-displacement plotted in a pair of orthogonal axes, all plots having the same abscissa. The maximax pseudo-velocity at a particular SDOF undamped natural frequency is thought to be more representative of the damage potential for a shock since it correlates with stress and strain in the elements of a single degree of freedom system (paragraph 6.1, reference f). If the testing is to be used for laboratory simulation, use

a Q value of ten and a second Q value of 50 in the processing. Using two Q values, a damped value and a value corresponding to light damping, provides an analyst with information on the potential spread of materiel response. It is recommended that the maximax absolute acceleration SRS be the primary method of display for the shock, with the maximax pseudo-velocity SRS the secondary method of display and useful in cases in which it is desirable to be able to correlate damage of simple systems with the shock. Figure 516.6-5 contrasts the maximax acceleration SRS for the Q values of 10 and 50 and for both  $T_E$  and  $T_e$  displayed in Figure 516.6-3. Figure 516.6-6 displays the same information in form of a pseudo-velocity SRS for a Q of 10 for both  $T_E$  and  $T_e$ . T<sub>e</sub> provides higher low frequency levels.



Figure 516.6-4. Response acceleration short-time root-mean-square with averaging time of 10% and 20% of  $T_{\rm e}$  .







Figure 516.6-6. Pseudo-Velocity SRS over  $T_{\rm E}\,$  and  $T_{\rm e}\,$  for Dynamic Quality Factor Q of 10.

Energy Spectral Density (ESD): The ESD estimate is a properly scaled magnitude squared of the c. Fourier Transform of the total shock. Its counterpart, the Fourier Spectra (FS), is in effect the square root of the ESD and may be useful for display but will not be discussed further here. The ESD is computed at a uniform set of frequencies distributed over the bandwidth of interest and displayed as a two-dimensional plot of amplitude units ("units<sup>2</sup> – sec/Hz") versus frequency in Hz. In determining the estimate the Fast Fourier Transform block size must include the entire shock above the instrumentation noise floor otherwise the low frequency components will be biased. Selection of an analysis filter bandwidth may require padding with zeros beyond the effective duration. Generally a rectangular window will be assumed in the time domain, however, other windows are permissible as long as the analyst understands the effects of the window shape in the frequency domain i.e., time domain multiplication results in frequency domain convolution. The ESD description is useful for comparing the distribution of energy within selected frequency bands among several shocks. Figure 516.6-7 displays the ESD estimate for the shock time history in Figure 516.6-1 for both T<sub>E</sub> and T<sub>e</sub>. At high frequencies the ESD values tend to be identical for both durations. For an ESD estimate, the percentage of normalized random error in the ordinate is approximately 100 percent. By either (1) averaging n adjacent ESD ordinates (keeping estimate bias a minimum) or (2) averaging n independent, but statistically equivalent ESD estimates, the percentage of normalized random error can be decreased by a factor of  $1/\sqrt{n}$ .



Figure 516.6-7. Energy Spectral Density Estimates over  $\,T_{\!_{\rm E}}\,$  and  $\,T_{\!_{\rm e}}\,.$ 

## 2.3.1.2 Shock/Random Vibration.

In general, any one test procedure will not be required along any axis for which a sufficiently severe random vibration test procedure is required, provided that system integrity requirements are comparable. Random vibration test severity is sufficient if the shock response spectrum over a short duration of the signal based upon a  $3\sigma$ Gaussian acceleration response of a SDOF, exceeds the shock test response spectrum everywhere in the specified range of natural frequencies. The Q value to be used in the analysis is generally taken to be ten; that is equivalent to five percent of critical viscous damping. It is well known (paragraph 6.1 references g, i, j) that the rms response at natural frequency  $f_n$  in Hz, of a single-degree-of-freedom linear oscillator with damping factor at  $f_n$ ,  $Q_n$  to a white noise random input,  $G(f_n)$  in  $g^2/Hz$ , is given as

$$RMS(f_n) = \left[\frac{\pi}{2}G(f_n)f_nQ_n\right]^{\frac{1}{2}}$$

so that the  $3\sigma$  amplitude is given as

 $A_{3\sigma}(f_n) = 3\left[\frac{\pi}{2}G(f_n)f_nQ_n\right]^{\frac{1}{2}}$ . For an amplification of unity this can be taken to approximate the maximax

shock response spectrum amplitude in g's. Annex C of this method discusses the relationship between ASD levels

and corresponding SRS levels for purposes of substituting a comparatively high level random vibration test for a relatively low level shock test.

## 2.3.1.3 Statistical Estimate Processing.

At times it may be convenient or even necessary to combine equivalently processed response estimates in some statistical manner. Paragraph 6.1, reference b, discusses some options in statistically summarizing processed results from a series of tests. The best option is dependent upon the size of sample in general. Processed results from the SRS, ESD, or FS are typically logarithmically transformed to provide estimates that are more normally distributed. This transformation is important since often very few estimates are available from a test series and the probability distribution of the untransformed estimates cannot be assumed to be normally distributed. In virtually all cases, combination of processed results will fall under the category of small sample statistics and need to be considered with care with other parametric or less powerful nonparametric methods of statistical analysis. Annex A addresses the appropriate techniques for the statistical combination of processed test results as a function of the size of the sample.

## 2.3.1.4 Other Processing.

Other descriptive processes that tend to decompose the shock into component parts, e.g., product model, time domain moments, wavelets, etc., may be useful, but are beyond the scope of this document.

## 2.3.2 Test conditions.

Derive the test SRS and  $T_e$  from statistical processing of (1) time history measurements of the materiel's functional environment, (2) from a carefully scaled measurement of a dynamically similar environment, (3) from prediction, or (4) from a combination of sources. For tailoring purposes, every attempt needs to be made to obtain measured data under conditions similar to service environment conditions in the Life Cycle Profile. In test SRS and  $T_e$  derivation and subsequent execution rank from the most desirable to the least desirable as follows:

- measured data summarized and shock created by way of direct reproduction of the measured data under exciter waveform control (see Method 525);
- measured data summarized and shock synthesized by way of a complex transient making sure that measured  $T_e$  is approximately the test  $T_e$ , and the measured waveform is similar to the synthesized waveform, i.e., amplitude and zero crossing similarity.
- no measured data but previous SRS estimates available and shock synthesized by way of a complex transient with T<sub>e</sub> specified in some reasonable way taking into consideration the natural frequency response characteristics of the materiel;
- no measured data but classical pulse shock descriptions available for use in reproducing the shock. (The use of classical pulse description is unacceptable unless use of such pulses can be justified on the basis of analysis.)
- a. <u>Measured data available</u>.  $T_e$  required for the test will be determined by examining representative time history measurements.  $T_e$  will extend from the first significant response time history point to the analytically derived  $T_e$  or to the noise floor of the instrumentation system, whichever is shortest. SRS

required for the test will be determined from analytical computations. For  $T_e < \frac{1}{2f_{min}}$ ,  $T_e$  for test may

be extended to  $\frac{1}{2f_{min}}$ . The SRS analysis will be performed on the AC coupled time history for Q = 10

at a sequence of natural frequencies spaced at 1/12 octave or less spacing to span at least 5 to 2,000 Hz.

(1) When a sufficient number of representative shock spectra are available, employ an appropriate statistical enveloping technique to determine the required test spectrum with a statistical basis (see

Annex A of this method). The T<sub>e</sub> for test should be taken as the maximum of the T<sub>e</sub> or  $\frac{1}{2f_{min}}$ ,

whichever is greater.

(2) When insufficient measured data are available for statistical analysis, use an increase over the maximum of the available spectral data to establish the required test spectrum. This should account for stochastic variability in the environment and uncertainty in any predictive methods employed.

The degree of increase is based on engineering judgment and should be supported by rationale. In these cases, it is often convenient to envelope the SRS estimates and proceed to add either a 3dB or 6dB margin to the SRS, depending on the degree of test level conservativeness desired (see Annex A paragraph 3.2. of this method). The  $T_e$  for test should be taken as the maximum of the  $T_e$  or

 $\frac{1}{2f_{min}}$  , whichever is greater.

Measured data not available. If a measured data base is not available, then for Procedure I - Functional b. Shock, and Procedure V - Crash Hazard Shock Test, employ the applicable SRS spectrum from Figure 516.6-8 as the test spectrum for each axis, provided  $T_e$  of the test shock time history falls between the values in the accompanying Table (516.6-I). This spectrum approximates that of the perfect terminalpeak sawtooth pulse. It is highly recommended that the test be performed with a waveform that is composed of either (1) a superposition of damped sinusoids with selected properties at a finite number of designated frequencies or (2) a superposition of amplitude modulated sine waves with selected properties at a finite number of designated frequencies, such that this waveform has an SRS that approximates the SRS on Figure 516.6-8 where the duration of this waveform is a maximum of  $T_e$ provided in Table 516.6-I. In reality, any complex test transient is suitable if it equals or exceeds this spectrum requirement over the frequency range of 5 to 2000 Hz, and meets the duration requirement. Use of the classical terminal-peak sawtooth pulse and the classical trapezoidal pulse is the least permissible test alternative in the case of no data being available (see paragraph 2.3.2c). In cases in which there is a vibration requirement for the materiel in addition to a shock requirement it may be possible to perform the vibration test in lieu of the shock test in the tailoring procedure. An example of this form of tailoring is contained in Procedure I - Functional Shock. Figure 516.6-9 provides two ASD curves to be used for comparison with specified ASD test environments to determine if random vibration is of sufficient severity to be used in lieu of measured or specified shock levels. The SRS for stationary random environments developed from these ASD curves, envelopes the appropriate SRS spectra on Figure 516.6-8. For some empirical justification of this, see Annex C of this method.

Test Category	Peak Acceleration (g's)	$T_e (ms)^{/1}$	Cross-over Frequency (Hz)
Functional Test for	20	15-23	45
Flight Equipment			
Functional Test for	40	15-23	45
Ground Equipment			
Crash Hazard Shock	40	15-23	45
Test for Flight			
Equipment			
Crash Hazard Shock	75	8-13	80
Test for Ground			
Equipment			

 Table 516.6-I.
 Test shock response spectra for use if measured data are not available.

Note 1: Refer to guidance in paragraph 2.3.3 c and d to customize the bandwidth of the SRS and Te.



Figure 516.6-8. Test SRS for use if measured data are not available (for Procedure I -Functional Shock, & Procedure V - Crash Hazard Shock Test).



Figure 516.6-9. Random test input ASD yielding equivalent test SRS spectrum shown on Figure 516.6-8 (for Procedure I - Functional Shock).

c. <u>Classical shock pulses (mechanical shock machine)</u>. Unless the procedure requires the use of a classical shock pulse, the use of such a pulse is not acceptable unless it can be demonstrated that measured data is within the tolerances of the classical shock pulses. Only two classical shock pulses are defined for testing in the method – the terminal peak sawtooth pulse, and the trapezoidal pulse. The terminal peak sawtooth pulse along with its parameters and tolerances are provided on Figure 516.6-10, and is an alternative for testing in Procedure I - Functional Shock and Procedure V - Crash Hazard Shock Test.



NOTE 1: Include in the time history display a time about  $3T_D$  long with a pulse located approximately in the center. The peak acceleration magnitude of the sawtooth pulse is  $A_m$  (expressed in units of g) and its duration is  $T_D$ . Ensure the measured acceleration pulse is contained between the broken line boundaries and the measured velocity change (that may be obtained by integration of the acceleration pulse) is within the limits of  $V_i \pm 0.1 V_i$ , where  $V_i$  is the velocity change associated with the ideal pulse that equals 0.5  $T_DA_m$  Extend the integration to determine velocity change from 0.4  $T_D$  before the pulse, to 0.1  $T_D$  after the pulse.

# Figure 516.6-10. Terminal peak sawtooth shock pulse configuration and its tolerance limits (for use when shock response spectrum analysis capability is not available in Procedure I – Functional Shock, and Procedure V - Crash Hazard Shock Test).

Table 516.6-II.	Terminal peak sawtooth	pulse test parameters	(refer to Figure 516.6-10).
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Test	Minimum (A <sub>m</sub>	Peak Value ) g's	Nominal Dur	ation (T <sub>D</sub> ) ms
	Flight Vehicle Equipment <sup>1</sup> a	Ground Equipment b	Flight Vehicle Equipment <sup>1</sup> c	Ground Equipment d
Functional Test	20	40 <sup>2</sup>	11	11

<sup>1</sup> Shock parameters a and c: Recommend for materiel not shock-mounted and weighing less than 136 kg (300 lbs).

<sup>2</sup> For materiel mounted only in trucks and semi-trailers, use a 20g peak value.

The trapezoidal pulse along with its parameters and tolerances is provided on Figure 516.6-11, and is an alternative for testing in Procedure II - Materiel to be Packaged, and Procedure III - Fragility.



NOTE 2: Include in the time history display a time about  $3T_D$  long with a pulse located approximately in the center. The peak acceleration magnitude of the trapezoidal pulse is  $A_m$  (expressed in units of g) and its duration is  $T_D$ . Ensure the measured acceleration pulse is between the broken line boundaries and the measured velocity change (that may be obtained by integration of the acceleration pulse) is within the limits of  $V_i \pm 0.1 V_i$ , where  $V_i$  is the velocity change associated with the ideal pulse that approximately equals  $0.5 A_m(2T_D-T_R-T_F)$ . The integration to determine velocity change extends from  $0.4T_D$  before the pulse to  $0.1 T_D$  after the pulse. Ensure the rise  $(T_R)$  and fall  $(T_F)$  times are less than or equal to  $0.1T_D$ .

# Figure 516.6-11. Trapezoidal shock pulse configuration and its tolerance limits (for use when shock response spectrum analysis capability is not available in Procedure II – Materiel to be Packaged, and Procedure III - Fragility).

		8 /
Test	Peak Value (A <sub>m</sub> ) g's	Nominal Duration (T <sub>D</sub> ) (sec)
Packaged Shock	30	$T_{D} = \frac{2\sqrt{2g}}{A_{m}}$

Table 516.6-III. Trapezoidal pulse parameters (refer to Figure 516.6-11).

d. <u>Classical shock pulses (vibration exciter)</u>. If a vibration exciter is to be employed in the conduct of a classical shock pulse, it will be necessary to optimize the reference pulse such that the net velocity and displacements are zero. Unfortunately, the need to compensate the reference pulse distorts the temporal and spectral characteristics, resulting in two specific problems that will be illustrated through example using a terminal peak sawtooth (the same argument is relevant for any classical pulse test to be conducted on a vibration exciter). First, a typical pre-pulse compensation of around 20% of the reference pulse peak will result in a time history that is outside of the 5% pre-pulse amplitude tolerances given in Figures 516.6-10 and 11. Second, as illustrated by the pseudo-velocity SRS in Figure 516.6-12, the velocities in the low frequency portion of the SRS will be significantly reduced in amplitude. Also, there is generally an area of increased amplitude associated with the duration of the pre-

compensation. Observe that the low frequency drop-off in SRS levels between the compensated and uncompensated pulse is readily identifiable and labeled  $f_1$ . Likewise, the frequency at which the compensated and uncompensated pulses converge is readily identifiable and labeled  $f_2$ . The drop-off at  $f_1$  is considered to be acceptable if and only if the lowest resonant frequency of the item being tested,  $f_N$ , is greater than  $f_1$  by a factor of two or more ( $f_N \ge 2^* f_1$ ). The amount of gain in the region  $f_1 \le f \le f_2$  is directly related to the duration and magnitude of the compensation pulse. The potential for over-test in this spectral band must also be carefully considered prior to proceeding.



Figure 516.6-12. Illustration of temporal and spectral distortion associated with a compensated classical terminal peak sawtooth

## 2.3.3 Test axes and number of shock events – general considerations.

Subject the test item to a sufficient number of suitable shocks to meet the specified test conditions at least three times in both directions along each of three orthogonal axes. A suitable test shock for each direction of each axis is defined to be one classical shock pulse or complex transient pulse that yields a response spectrum that is within the tolerances of the required test spectrum over the specified frequency range, and when the effective duration of the shock is within twenty percent of the specified  $T_e$  value. Determine the spectra for positive and negative maximum accelerations (either maximum absolute or equivalent static), generally at Q = 10, and at least 1/12-octave frequency intervals. If the required test spectrum can be satisfied simultaneously in both directions along an axis, three shock repetitions will satisfy the requirement for that axis. If the requirement can only be satisfied in one direction, i.e., polarity consideration for classical shock inputs, it is permissible to change the test setup and impose three additional shocks to satisfy the spectrum requirement in the other direction. Setup change possibilities are to (1) reverse the polarity of the test shock time history or (2) to reverse the test item orientation (in general, for complex transient pulses, reversal of the polarity of the test shock time history will not significantly affect the test levels). The following guidelines may also be applied for either classical shock pulses or complex transient pulses.

- a. For materiel that is likely to be exposed only rarely to a given shock event, perform one shock for each appropriate environmental condition: one shock per axis minimum or two shocks per axis if polarity charge is a consideration. For large velocity change shock conditions, perform one shock for each appropriate environmental condition.
- b. For materiel that is likely to be exposed more frequently to a given shock event and there is little available data to substantiate the number of shocks, apply three or more at each environmental condition based on the anticipated in-service use, three shocks per axis minimum or six shocks per axis if polarity charge is a consideration.
- c. If the test item has no significant low frequency modal response then it is permissible to allow the low frequency portion of the SRS to fall out of tolerance in order to satisfy the high frequency portion of the SRS provided the high frequency portion begins at least one octave below the first natural mode frequency ( $f_{min}$ ) of the test item. Keep the duration within tolerance.
- d. If the test item has significant low frequency modal response, then it is permissible to allow the duration of the complex transient pulse to fall outside of the  $T_e$  range, provided in Table 516.6-I, in order to satisfy the low frequency portion of the SRS. The effective duration contained in Table 516.6-I may be

increased by as much as  $\frac{1}{2f_{min}}$  over Te in order to have the low frequency portion of the SRS within

tolerance.

## 2.3.4 Special considerations for complex transients.

There is no unique synthesized complex transient pulse satisfying a given SRS. In synthesizing a complex transient pulse from a given SRS and this complex transient pulse either (1) exceeds the capability of the shock application system (usually in displacement or velocity), or (2) the duration of the complex transient pulse is more than 20 percent longer than  $T_e$ , some compromise in spectrum or duration tolerance may be necessary. It is unacceptable to decompose a SRS into a low frequency component (large velocity and displacement) and a high frequency component to meet a shock requirement. Often an experienced analyst may be able to specify the input parameters to the complex transient pulse synthesis algorithm in order to satisfy the requirement for which the shock application system manufacturer "optimum" solution will not. The following guidelines may be applied.

- a. If the test item has no significant low frequency modal response, it is permissible to allow the low frequency portion of the SRS to fall out of tolerance in order to satisfy the high frequency portion of the SRS, provided the high frequency portion begins at least one octave below the first natural mode frequency of the test item. Keep the duration within tolerance.
- b. If the test item has significant low frequency modal response, it is permissible to allow the duration of the complex transient pulse to fall out of tolerance in order to satisfy the low frequency portion of the SRS, provided the duration of the complex transient pulse does not exceed  $T_e + 1/(2f_{min})$  where the latter term is one half the period of the lowest frequency of interest ( $f_{min}$ ) in the SRS analysis. If the duration of the complex transient pulse must exceed  $T_e + 1/(2f_{min})$  in order to have the low frequency portion of the SRS within tolerance, use a new shock procedure.

## 2.4 Test Item Configuration.

(See Part One, paragraph 5.8.) The configuration of the test item strongly affects test results. Use the anticipated configuration of the materiel in the life cycle profile. As a minimum, consider the following configurations:

- a. In a shipping/storage container or transit case.
- b. Deployed in the service environment.

## 3. INFORMATION REQUIRED.

## 3.1 Pretest.

The following information is required to conduct a shock test.

- a. <u>General</u>. Information listed in Part One, paragraphs 5.7, 5.9, and 5.11 of this standard, and in Part One, Annex A, Task 405.
- b. Specific to this method.
  - (1) Test fixture modal survey procedure.
  - (2) Test item/fixture modal survey procedure.
  - (3) Shock environment. Either:
    - (a) the predicted SRS or the complex shock pulse synthesis form (superposition of damped inusoids, amplitude modulated sine waves, or other) specifying spectrum shape, peak spectrum values, spectrum break points, and pulse duration, or
    - (b) the measured data selected for use in conjunction with the SRS synthesis technique outlined in the procedures. (If the SRS synthesis technique is used, ensure both the spectral shape and synthesized shock duration are as specified.), or
    - (c) the measured data that are input as a compensated waveform into an exciter/shock system under direct waveform control. (See Method 525.)
  - (4) Techniques used in the processing of the input and the response data.
  - (5) Note all details of the test validation procedures
- c. <u>Tailoring</u>. Necessary variations in the basic test procedures to accommodate LCEP requirements and/or facility limitations.

## 3.2 During Test.

Collect the following information during conduct of the test:

- a. <u>General</u>. Information listed in Part One, paragraph 5.10 and in Part One, Annex A, Task 406 of this standard.
- b. <u>Specific to this Method</u>. Information related to failure criteria for test materiel under acceleration for the selected procedure or procedures. Pay close attention to any test item instrumentation and the manner in which the information is received from the sensors. For large velocity shock, ensure instrumentation cabling does not add noise to measurements as a result of cable movement.
- c. If measurement information is obtained during the test, examine the time history traces and process according to procedures outlined in the test plan.

## 3.3 Post-test.

The following information shall be included in the test report.

- a. <u>General</u>. Information listed in Part One, paragraph. 5.13 of this standard, and in Part One, Annex A, Task 406.
- b. Specific to this method.
  - (1) Duration of each exposure and number of exposures.
  - (2) Status of the test item after each visual examination.
  - (3) Response time histories and the information processed from these time histories. In general, under-processed information, the absolute acceleration maximax SRS, and the pseudo-velocity SRS should be supplied as a function of single degree of freedom oscillator undamped natural frequency. In certain cases, the ESD and FS may be supplied.
  - (4) Test item and/or fixture modal analysis data.
  - (5) Any deviation from the test plan.

## 4. TEST PROCESS.

## 4.1 Test Facility.

Use a shock-producing apparatus capable of meeting the test conditions as determined according to the appropriate paragraphs of this method. The shock apparatus may be of the free fall, resilient rebound, nonresilient rebound, hydraulic, compressed gas, electrodynamic exciter, electrohydraulic exciter, or other activating types capable of eliciting test item response over the time, amplitude and frequency ranges specified. For all types of shock-producing apparatus, careful attention needs to be paid to the time, amplitude, and frequency ranges over which the apparatus is capable of delivering a shock input. For example, an electrohydraulic exciter may have only a DC to 500 Hz controllable frequency reproduction range. Procedures II and III require test apparatus capable of producing relatively large displacement. Procedure VII is a special test setup in which large containers impact a rigid barrier. Procedure VIII for catapult launch is best satisfied by application of two shock pulses with an intervening "transient vibration."

## 4.2 Controls.

## 4.2.1 Calibration.

The shock apparatus will be user calibrated for conformance with the specified test requirement from the selected procedure where the response measurements will be made with traceable laboratory calibrated measurement devices. Conformance to test specifications will, in general, use a "calibration load" in the test setup. The calibration load will, in general, be a mass/stiffness simulant of the test item. "Mass/stiffness simulants" imply that the modal dynamic characteristics of the test item are replicated to the extent possible in the simulant – particularly those modal dynamic characteristics that may interact with the modal dynamic configuration load that satisfy the test conditions outlined in Procedures I, II, III, V, VI, or VIII. Procedure IV is not a calibrated test. After processing the measured response data from the calibration load and verifying that it is in conformance with the test specification tolerances, remove the calibration load and perform the shock test on the test item. Use of calibration loads for setup is highly recommended in all cases.

## 4.2.2 Tolerances.

For test validation, use the tolerances specified under each individual procedure, along with the guidelines provided below. In cases in which such tolerances cannot be met, establish achievable tolerances that are agreed to by the cognizant engineering authority and the customer prior to initiation of test. In any case, where tolerances are established independently of the guidance provided below, establish those tolerances that are within the limitations of the specified measurement calibration, instrumentation, signal conditioning, and data analysis procedures.

## 4.2.2.1 Classical pulses and complex transient pulses-time domain.

For the classical pulses of the terminal-peak sawtooth pulse and the trapezoidal pulse tolerance limits on the time domain representation of the pulses (both for amplitude and duration) are as specified in Figures 516.6-10 and 516.6-11, respectively. For complex transient pulses specified in the time domain the major peaks and valleys of the measured pulses, (peaks and valleys within 75 percent of the maximum peak and valley specified, respectively) 90 percent of the peak and valley levels are to be within  $\pm 10$  percent of the specified peaks and valleys, respectively. This tolerance limit assumes that the shock test machine is able to replicate the specified shock accurately under a waveform control procedure. Such time domain specification is useful for shock replication from measured data and for fragility tests performed using an electrodynamic or electrohydraulic test machine. Inherent in the tolerance specification is the assumption that the measured peak and valley sequence is ordered as the specified peak and valley time history peak and valley sequence.

## 4.2.2.2 Complex transient pulses-SRS.

For complex transient pulses specified by way of the maximax SRS on Figure 516.6-8 and for the other complex transient pulses specified from measured data, generally, the tolerances are specified in terms of amplitude over a specified frequency bandwidth and a tolerance on the pulse duration. If prior measured data are available, or a series of shocks are performed, all acceleration maximax SRS computed with a one-twelfth octave frequency resolution are to be within -1.5 dB and +3dB over a minimum of 90 percent of the overall frequency bandwidth from 10 Hz to 2 kHz. For the remaining 10 percent part of the frequency band, all SRS are to be within -3dB and +6dB. The duration of the complex transient is to be within  $\pm 20$  percent of the effective duration of the measured pulse, T<sub>e</sub>. In addition, the following guidance is provided for use of (1) the pseudo-velocity response spectra and (2) multiple measurements to specify a shock environment. All tolerances are specified on the maximax

acceleration SRS. Any tolerances specified on the pseudo-velocity response spectra must be derived from the tolerances on the maximax acceleration SRS and be consistent with those tolerances including tolerance on the duration of the pulse. The test tolerances are stated in terms of a single measurement tolerance. For an array of measurements defined in terms of a "zone" (paragraph 6.1, reference b), amplitude tolerance may be specified in terms of an average of the measurements within a "zone." However, this is, in effect, a relaxation of the single measurement tolerance, and even though individual measurements may be substantially out of tolerance while the average is within tolerance. In general, when specifying test tolerances based on averaging for more than two measurements within a zone, the tolerance band should not exceed the 95/50 one-sided normal tolerance upper limit computed for the logarithmically transformed SRS estimates nor be less than the mean minus 1.5dB. Any use of "zone" tolerances and averaging must have support documentation prepared by a trained analyst. The tolerance on the duration of the pulse applies to the input pulse duration to the measurement array.

## 4.3 Test Interruption.

Test interruptions can result from two or more situations, one being from malfunction of test chambers or associated test laboratory equipment. The second type of test interruption results from malfunction of the test item itself during operational checks.

## **4.3.1** Interruption due to facility malfunction.

- a. <u>General</u>. See Part One, paragraph 5.11 of this standard.
- b. <u>Specific to this method</u>. Interruption of a shock test is unlikely to generate any adverse effects. Normally, continue the test from the point of interruption.

## **4.3.2** Interruption due to test item operation failure.

Failure of the test item(s) to function as required during operational checks presents a situation with several possible options.

- a. The preferable option is to replace the test item with a "new" one and restart from Step 1.
- b. A second option is to replace / repair the failed or non-functioning component or assembly with one that functions as intended, and restart the entire test from Step 1.

**NOTE**: When evaluating failure interruptions, consider prior testing on the same test item, and consequences of such.

## 4.4 Instrumentation.

In general, acceleration will be the quantity measured to meet the specification. On occasion other devices may be employed, e.g., linear displacement/voltage transducer, force gage, laser velocimeter, rate gyro, etc. In these cases, give special consideration to the instrument specification to satisfy the calibration, measurement, and analysis requirements. Calibrate all measurement instrumentation to traceable national calibration standards (see Part One, paragraph 5.3.2). In addition, instrumentation to measure test item function may be required. In this case, obtain suitable calibration standards and adhere to them.

- a. <u>Accelerometer</u>.
  - (1) Transverse sensitivity of less than or equal to 5 percent.
  - (2) An amplitude linearity within 10 percent from 5 percent to 100 percent of the peak acceleration amplitude required for testing.
  - (3) For Procedures I, II, III, IV, V, VI, and VIII, a flat frequency response within ±5 percent across the frequency range 2 Hz 2000 kHz.
  - (4) For cases in which response below 2 Hz is desired, piezoresistive accelerometer measurement is required with a flat frequency response within  $\pm 5$  percent across the measurement specification bandwidth.
  - (5) The measurement device and its mounting will be compatible with the requirements and guidelines provided in paragraph 6.1, reference a.
- b. <u>Other measurement devices</u>. Any other measurement devices used to collect data must be demonstrated to be consistent with the requirements of the test, in particular, the calibration and tolerance information provided in paragraph 4.2.
- c. <u>Signal conditioning</u>. Use only signal conditioning that is compatible with the instrumentation requirements of the test, and is compatible with the requirements and guidelines provided in paragraph

6.1, reference a. In particular, filtering of the analog voltage signals will be consistent with the time history response requirements (in general, demonstrable linearity of phase throughout the frequency domain of response), and the filtering will be so configured that anomalous acceleration data caused by clipping will not be misinterpreted as response data. In particular, use extreme care in filtering the acceleration signals at the amplifier output. Never filter the signal into the amplifier for fear of filtering bad measurement data, and the inability to detect the bad measurement data. The signal from the signal conditioning must be anti-alias filtered before digitizing.

## 4.5 Data Analysis.

- a. An analog anti-alias filter configuration will be used that will:
  - (1) not alias more than a 5 percent measurement error into the frequency band of interest.
  - (2) have linear phase-shift characteristics in the data passband.
  - (3) have a pass band uniform to within one dB across the frequency band of interest.
- b. In subsequent processing of the data, use any additional digital filtering that is compatible with the antialias analog filtering. In particular, additional digital filtering must maintain phase linearity for processing of shock time histories.
- c. Analysis procedures will be in accordance with those requirements and guidelines provided in paragraph 6.1, reference a. In particular, validate the shock acceleration amplitude time histories according to the procedures in paragraph 6.1, reference a. Integrate each amplitude time history to detect any anomalies in the measurement system, e.g., cable breakage, amplifier slew rate exceedance, data clipped, unexplained accelerometer offset, etc., before processing the response time histories. If anomalies are detected, discard the invalid measured response time history data.

## 4.6 Test Execution.

## 4.6.1 Preparation for test.

## 4.6.1.1 Preliminary guidelines.

Prior to initiating any testing, review the pretest information in the test plan to determine test details (e.g., procedure, calibration load, test item configuration, measurement configuration, shock level, shock duration, and number of shocks to be applied). Note all details of the test validation procedures.

## 4.6.1.2 Pretest checkout.

After calibration of the excitation input device and prior to conducting the test, perform a pretest checkout of the test item at standard ambient conditions to provide baseline data. Conduct the checkout as follows:

- Step 1. Conduct a complete visual examination of the test item with special attention to stress areas or areas identified as being particularly susceptible to damage and document the results.
- Step 2. Where applicable, install the test item in its test fixture.
- Step 3. Conduct a test item operational check in accordance with the approved test plan, and document the results for compliance with Part One, paragraph 5.15.
- Step 4. If the test item operates satisfactorily, proceed to the first test. If not, resolve the problem and restart at Step 1.

## 4.6.1.3 Procedures' overview.

Paragraphs 4.6.2 through 4.6.9 provide the basis for collecting the necessary information concerning the system under shock. For failure analysis purposes, in addition to the guidance provided in Part One, paragraph 5.14, each procedure contains information to assist in the evaluation of the test results. Analyze any failure of a test item to meet the requirements of the system specifications, and consider related information such as follows in paragraphs 4.6.2 through 4.6.9.

## 4.6.2 Procedure I - Functional Shock.

The intent of this test is to disclose materiel malfunction that may result from shocks experienced by materiel during use in the field. Even though materiel has successfully withstood even more severe shocks during shipping or transit shock tests, there are differences in support and attachment methods and in functional checking requirements that make this test necessary. Tailoring of the test is required when data are available, can be measured, or can be estimated from related data using accepted dynamic scaling techniques. When measured field data are not available for tailoring, use the information in Figure 516.6-8 and the accompanying Table 516.6-I to define the shock test

system input SRS. In the calibration procedure, the calibration load will be subject to a properly compensated complex waveform in accordance with the SRS described above for electrodynamic or electrohydraulic shock testing. In general, tests using classical pulses, e.g., half-sine, terminal peak sawtooth, etc., are unacceptable unless it can be demonstrated during tailoring that the field shock environment approximates such a form. If all other testing resources have been exhausted, it will be permissible to use the information on Figure 516.6-10 for the terminal peak sawtooth for testing. However, such testing must be performed in both a positive and negative direction. In cases in which the test item has been exposed to random vibration prior to shock testing, Figure 516.6-9 presents ASD requirements that provide for "equivalent test SRS." If the prior random vibration levels meet or exceed the ASD levels provided in Figure 516.6-8, the functional shock test may be waived under approval of the cognizant test authority. However, functional test requirements must be the same between the vibration and the proposed shock test.

## 4.6.2.1 Controls.

Figure 516.6-8 provides predicted input SRS for the functional shock test for use when measured data are not available, and when the test item configuration falls into one of two specified categories – (1) flight equipment, or (2) ground equipment. The duration,  $T_e$ , is defined in paragraph 2.3.1, and is specified in Table 516.6-I. Figure 516.6-9 provides the predicted random vibration test input ASDs that yield the equivalent SRS given on Figure 516.6-8. If the prior random vibration levels meet or exceed the ASD levels provided on Figure 516.6-9, the functional shock test may be waived. Functional test requirements must be the same between the vibration and the shock tests.

## 4.6.2.2 Test tolerances.

For complex transients from measured data, ensure that test tolerances are consistent with the general guidelines provided in paragraph 4.2.2 with respect to the information provided in Table 516.6-I and accompanying Figure 516.6-8. For random test input ASD yielding an equivalent test SRS spectrum, the lower tolerance band on the ASD of Figure 516.6-9 is to be -1dB over the entire frequency band of interest, with no specification for the upper tolerance band (generally when the equivalence testing is used it is because the vibration requirement is substantially more severe than that defined by the ASD spectra on Figure 516.6-9). Annex C provides additional information related to the empirical spread of the maximax SRS for Q=5 given the ASD inputs on Figure 516.6-9.

For classical pulse testing, the test tolerances are specified on Figure 516.6-10 with respect to information in Table 516.6-II.

## 4.6.2.3 Procedure I – Functional Shock

Step 1. Select the test conditions and calibrate the shock test apparatus as follows:

- a. Select accelerometers and analysis techniques that meet or exceed the criteria outlined in paragraph 4.3 of paragraph 6.1, reference a.
- b. Mount the calibration load to the shock test apparatus in a configuration similar to that of the test item. If the materiel is normally mounted on vibration/shock isolators, ensure the corresponding test item isolators are functional during the test. If the shock test apparatus input waveform is to be compensated via input/output impulse response function for waveform control, exercise care to details in the calibration configuration and the subsequent processing of the data.
- c. Perform calibration shocks until two consecutive shock applications to the calibration load produce waveforms that meet or exceed the derived test conditions consistent with the test tolerances in paragraph 4.6.2.2 for at least the test direction of one axis.
- d. Remove the calibration load and install the test item on the shock apparatus.
- Step 2. Perform a pre-shock operational check of the test item. If the test item operates satisfactorily, proceed to Step 3. If not, resolve the problems and repeat this step.
- Step 3. Subject the test item (in its operational mode) to the test shock input.
- Step 4. Record necessary data to show that the shock met or exceeded desired test levels within the specified tolerances in paragraph 4.6.2.2. This includes test setup photos, test logs, and photos of actual shocks from the transient recorder or storage oscilloscope. For shock and vibration isolated assemblies inherent within the test item, make measurements and/or inspections to assure these

assemblies did not impact with adjacent assemblies. If required, record the data to show that the materiel functions satisfactorily during shock.

- Step 5. Perform a post test operational check on the test item. Record performance data. If the test item does not operate satisfactorily, follow the guidance in paragraph 4.3.2 for test item failure.
- Step 6. Repeat Steps 2, 3, 4, and 5 two additional times for each orthogonal test axis if the SRS form of specification is used (a total of three shocks in each orthogonal axis). If the classical shock form of specification is used, subject the test item to both a positive and a negative input pulse (a total of six shocks in each orthogonal axis). If one or both of the test pulse's time history or SRS falls outside the pulse time history tolerance or the SRS test tolerance, continue to tailor the pulses until both test tolerances are met. If both test tolerances cannot be met simultaneously, choose to satisfy the SRS test tolerance.
- Step 7. Perform a post test operational check on the test item. Record performance data, document the test sequence, and see paragraph 5 for analysis of results.

## 4.6.3 Procedure II - Materiel to be Packaged.

The intent of this test is to ensure the functionality of materiel after it has been inadvertently dropped before, during, or after a packaging process. In general, such input to the materiel produces large velocities and large changes in velocity. For this procedure, the classical trapezoidal pulse may be used on properly calibrated drop machines if the large velocity/velocity change exceeds that available on standard electrodynamic and electrohydraulic test equipment. However, if the large velocity/velocity change is compatible with the capabilities of electrodynamic and/or electrohydraulic test equipment, consider tailoring the shock according to a complex transient for application on the electrohydraulic test equipment is acceptable if there are no available measured data contrary to the response time history form for this approach. In any case, when data are available or can be measured, or can be estimated from related data, tailor the test using accepted dynamic scaling techniques.

#### 4.6.3.1 Controls.

For application of the classical trapezoidal pulse subject the unpackaged test item in a nonoperational mode to a series of trapezoidal 30-g shock pulses, i.e.,  $A_m = 30g$ , having a time duration (in seconds) to be determined from Table 516.6-III and the equation

$$T_{D} = \frac{2\sqrt{2g}}{A_{m}}$$

where h is the design drop height and g is the acceleration of gravity. The equation for  $T_D$  assumes a 100 percent elastic rebound. The pulse will be in accordance with Figure 516.6-11. Because of the substantial displacement and velocity requirements, a programmable shock machine or a long stroke electrohydraulic exciter will more than likely be required to reproduce these test conditions. The trapezoidal pulse shape was chosen because:

- (1) computation of velocity change it produces (for comparison with design drop height is much easier to make and more reproducible than most shock spectrum synthesis routines that allow for more general pulses).
- (2) trapezoidal pulse shape provides an upper bound on primary and maximax SRS for a given peak acceleration input level where the primary SRS is defined to be the SRS over the duration of the pulse only.

For a tailored test using a complex waveform with SRS shock control, ensure the test input to the item is within specified test tolerances.

#### 4.6.3.2 Test tolerances.

For complex transients from measured data, ensure test tolerances are consistent with the general guidelines provided in paragraph 4.2.2. For classical pulse testing, ensure the test tolerances specified in Figure 516.6-11, with respect to the information provided in Table 516.6-III, are satisfied.

## 4.6.3.3 Procedure II – Materiel to be Packaged.

- Step 1. Calibrate the shock machine as follows:
  - a. Mount the calibration load to the test apparatus in a configuration similar to that of the actual test item. Use a fixture similar in shape and configuration to the shock attenuation system that will support the materiel in its shipping container. The fixture should be as rigid as possible to prevent distortion of the shock pulse input to the test item. If the test apparatus input waveform is to be compensated via input/output impulse response function, exercise care to details in the calibration configuration and the subsequent processing of the data.
  - b. Perform calibration shocks until two consecutive shock applications to the calibration load reproduce waveforms that are within the test tolerance specification.
- Step 2. Remove the calibration load and install the actual test item on the shock apparatus.
- Step 3. Perform a pre-shock operational test of the test item. If the test item operates satisfactorily, proceed to Step 4. If not, resolve the problems and repeat this step.
- Step 4. Subject the test item to the test pulse.
- Step 5. Record necessary test data to include test setup photos, test logs, and photos of the actual test pulse from a transient recorder or storage oscilloscope.
- Step 6. For classical trapezoidal shock waveform, repeat Steps 3, 4, and 5once in each direction for three orthogonal axes with positive and negative polarity (six shocks total). For a complex shock waveform, repeat Steps 3, 4, and 5 once in each of the three orthogonal axes (three shocks total).
- Step 7. Perform a post shock operational test of the test item. See paragraph 5 for analysis of results. Document the results, including plots of the measured test response waveforms and any pre- or post-shock operational anomalies.

Package Gross Weight, kg	Type of Handling	Design Drop	Maximum Test Item Velocity
( <b>lb</b> )		Height, cm (in)	Change <sup>*</sup> cm/s (in/s)
0 to 9.1 (0 to 20)	Manual	76 (30)	772 (304)
9.2 to 18.2 (21 to 40)	Manual	66 (26)	719 (283)
18.3 to 27.2 (41 to 60)	Manual	61 (24)	691 (272)
27.4 to 36.3 (61 to 80)	Manual	46 (18)	600 (236)
36.4 to 45.4 (81 to 100	Manual	38 (15)	546 (215)
45.5 to 68.1 (101 to 150	Mechanical	31 (12)	488 (192)
68.2 to 113.5 (151 to 250)	Mechanical	26 (10)	447 (176)
113.6 - (251 - )	Mechanical	20 (8)	399 (157)

Table 516.6-IV. Suggested drop height for Procedure II.

<sup>\*</sup>For an assumed 100 percent elastic rebound.

## 4.6.4 Procedure III - Fragility.

The intent of this test is to determine (1) the maximum level of input to which the materiel can be exposed and still continue to function as required by its operational guide without damage to the configuration or, (2) determine the minimum level of input on which exposure to a higher level of input will most likely result in either functional failure or configuration damage. Determination of the fragility level is accomplished by starting at a benign level of shock and proceeding to increase the level of shock to the test item until:

- a. failure of the test item occurs.
- b. a predefined test objective is reached without failure of the test item.
- c. a critical level of shock is reached that indicates failure is certain to occur at a higher level of shock.

(Paragraph 4.6.4c. above implies that an analysis of the materiel has been completed prior to testing, that critical elements have been identified with their "stress thresholds," and that a failure model of the materiel relative to the shock input level has been developed. In addition, during the test, the "stress thresholds" of these critical elements can be monitored, and input to a failure model to predict failure at a given shock input level.). In general, such input to the materiel produces large velocities and large changes in velocity. For this procedure, the classical trapezoidal pulse may be used on properly calibrated drop machines, if the large velocity/velocity change exceeds that available on standard electrodynamic and/or electrohydraulic test equipment. However, if the large

velocity/velocity change is compatible with the capabilities of electrodynamic and/or electrohydraulic test equipment, consider tailoring the shock according to a complex transient for application on the electrodynamic or electrohydraulic test equipment. Using a trapezoidal pulse on electrodynamic and/or electrohydraulic test equipment is acceptable if there are no available data, providing shock input information that is tailorable to a complex transient. For testing, note that there is a single parameter (peak amplitude of the shock input) to define the fragility level holding the maximum velocity change of the test shock approximately constant. In the case of SRS synthesis, maximum velocity change is not as well defined, nor as important, nor as easily controllable as for the classical trapezoidal pulse. Tailoring of the test is required when data are available, can be measured, or can be estimated from related data using accepted dynamic scaling techniques. An inherent assumption in the fragility test is that damage potential increases linearly with input shock level. If this is not the case, other test procedures may need to be used for establishing materiel fragility levels.

#### 4.6.4.1 Controls.

a. Select a design drop height, h, based on measurement of the materiel's shipping environment, or from Table 516.6-IV when measured data are unavailable. (A design drop height is the height from which the materiel might be dropped in its shipping configuration and be expected to survive.) A maximum test item velocity change may be taken from Table 516.6-IV, or determined by using the following relationship:

$$\Delta V = 2\sqrt{2gh}$$

where

- $\Delta V$  = maximum product velocity change cm/s (in/s) (summation of impact velocity and rebound velocity)
- h = design drop height cm (in)

 $g = 980.6 \text{ cm/s}^2 (386 \text{ in/s}^2)$ 

The maximum test velocity change assumes 100 percent rebound. Programming materials, other than pneumatic springs, may have less than 100 percent rebound, so the maximum test velocity needs to be decreased accordingly. If the maximum test velocity specified is used for drop table shock machine programming materials other than pneumatic springs, the test is conservative (an overtest), and the maximum test item velocity is a bounding requirement.

b. Set the shock machine to a maximum acceleration level  $(A_m)$  well below the anticipated fragility level (see Table 516.6-V). Determine the appropriate pulse duration from the design drop height, h, and the expression for  $T_D$  in paragraph 4.6.3.1. If an initial value for  $A_m$  does not exist, use 15g's. If no damage occurs, increase  $A_m$  incrementally while holding the maximum test item velocity change constant (i.e., decrease the pulse duration) until damage to the test item occurs. This will establish the materiel's critical acceleration fragility level.

Table 516.6-V.	Trapezoidal	pulse test	parameters	(refer to	Figure 516.6	-11).
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Test	Peak Value (A <sub>m</sub> ) g's	Nominal Duration (T <sub>D</sub> ) (sec)
Fragility	10 to 50	$T_{D} = \frac{2\sqrt{2g}}{Am}$

c. Test levels used in this procedure represent the correlation of the best information currently available from research and experience. Use more applicable test level data if they become available (paragraph 6.1, reference h). In particular, if data are collected on a materiel drop and the SRS of the environment computed, a scaled version of the SRS could be used to establish the acceleration fragility level with respect to a measured environment on electrodynamic or electrohydraulic test equipment, provided the displacement and velocity limitations of the test equipment are not exceeded, and the maximum test item velocity change can be held approximately constant. In addition to the maximax acceleration response spectra, compute the pseudo-velocity response spectra.

## 4.6.4.2 Test tolerances.

It is assumed that the instrumentation noise in the measurements is low so that tolerances may be established. For complex transients from measured data, ensure test tolerances are consistent with the general guidelines provided in paragraph 4.2.2. For classical pulse testing, ensure the test tolerances specified in Figure 516.6-11 with respect to the information provided in Table 516.6-V are satisfied.

## 4.6.4.3 Procedure III - Fragility.

This test is designed to build up in severity until a test item failure occurs, or a predetermined goal is reached. It may be necessary to switch axes between each shock event unless critical axes are determined prior to test. In general, all axes of importance will be tested at the same level before moving to another level. The order of test activity and the calibration requirements for each test setup should be clearly established in the test plan. It is also desirable to pre-select the steps in severity based on knowledge of the materiel item or the test environment, and document this in the test plan. Unless critical stress thresholds are analytically predicted and instrumentation used to track stress threshold buildup, there is no rational way to estimate the potential for stress threshold exceedance at the next shock input level. The following procedures, one for a classical pulse and the other for a complex transient, are written as if the test will be conducted in one axis alone. In cases where more test axes are required, modify the procedure accordingly.

- a. Classical Pulse. This part of the procedures assumes that the classical pulse approach is being used to establish the fragility level by increasing the drop height of the test item, thereby increasing the  $\Delta V$ directly. The fragility level is given in terms of the measurement variable-peak acceleration of the classical pulse.
  - Step 1. Mount the calibration load to the test apparatus in a configuration similar to that of the actual test item. Use a fixture similar in configuration to the interface of the shock attenuation system (if any) that will support the materiel. The fixture should be as rigid as possible to prevent distortion of the shock pulse input to the test item.
  - Perform calibration shocks until two consecutive shock applications to the calibration load Step 2. reproduce the waveforms that are within the specified test tolerances. If response to the calibration shock is nonlinear with respect to shock input level, other test procedures may need to be applied to establish materiel fragility levels depending upon the extent of the nonlinearity prior to reaching the "stress threshold."
  - Step 3. Select a drop height low enough to assure that no damage will occur. For drop heights other than those in Table 516.6-IV, the maximum velocity change can be taken to be

$$\Delta V = 2\sqrt{2gh}$$

Where

- $\Delta V =$ maximum test item velocity change, cm/s (in/s) (assumes full resilient rebound of test item)
  - drop height, cm (in) =
- h acceleration of gravity 981 cm/s<sup>2</sup> (386 in/s<sup>2</sup>) = g
- Mount the test item in the fixture. Perform an operational check and document the pre-test Step 4. condition. If the test item operates satisfactorily, proceed to Step 5. If not, resolve the problems and repeat this step.
- Perform the shock test at the selected level, and examine the recorded data to assure the test is Step 5. within tolerance.
- Visually examine and operationally check the test item to determine if damage has occurred. Step 6. If the test item does not operate satisfactorily, follow the guidance in paragraph 4.3.2 for test item failure.
- If it is required to determine the fragility of the test item in more than one axis, proceed to test Step 7. the item (Steps 4-6) in the other axes (before changing the drop height).
- Step 8. If the test item integrity is preserved, select the next drop height.
- Step 9. Repeat Steps 4 through 8 until the test objectives have been met.

- Step 10. Perform a post shock operational test of the test item. See paragraph 5 for analysis of results. Document the results, including plots of the measured test response waveforms, and any pre- or post-shock operational anomalies.
- b. Synthesized Pulse.

This part of the procedure assumes that the fragility level is some function of the peak acceleration level determined from a maximax acceleration SRS of a complex transient. For a complex transient specified in the time domain, this procedure could use the peak acceleration of the time history to define the fragility level.

- Step 1. Mount the calibration load to the test apparatus in a configuration similar to that of the actual test item. Use a fixture similar in configuration to the interface of the shock attenuation system (if any) that will support the materiel. The fixture should be as rigid as possible to prevent distortion of the shock pulse input to the test item.
- Step 2. Perform calibration shocks until two consecutive shock applications to the calibration load reproduce maximax acceleration SRS that are within the specified test tolerances. If response to the calibration shock is nonlinear with respect to shock input level, other test procedures may need to be applied to establish materiel fragility levels, depending upon the extent of the nonlinearity prior to reaching the "stress threshold."
- Step 3. Select a peak maximax acceleration SRS level low enough to assure no damage will occur.
- Step 4. Mount the test item in the fixture. Inspect and operationally test the item to document the pretest condition. If the test item operates satisfactorily, proceed to Step 5. If not, resolve the problems and repeat this step.
- Step 5. Perform the shock test at the selected level, and examine the recorded data to assure the test maximax acceleration SRS is within tolerance.
- Step 6. Visually examine and operationally check the test item to determine if damage has occurred. If so, follow the guidance in paragraph 4.3.2 for test item failure.
- Step 7. If it is required to determine the fragility of the test item in more than one axis, proceed to test the item in the other axes (before changing the peak maximax acceleration SRS level).
- Step 8. If the test item integrity is preserved, select the next predetermined peak maximax acceleration SRS level.
- Step 9. Repeat Steps 5 through 8 until the test objectives have been met.
- Step 10. Perform a post shock operational test of the test item. See paragraph 5 for analysis of results. Document the results, including plots of the measured test response waveforms and any pre- or post-shock operational anomalies.

## 4.6.5 Procedure IV - Transit Drop.

The intent of this test is to determine the structural and functional integrity of the materiel to a transit drop either outside or in its transit or combination case. Perform all tests with a quick release hook or drop tester. In general, there is no instrumentation calibration for the test and measurement information is minimized, however, if measurements are made, the maximax acceleration SRS and the pseudovelocity SRS will define the results of the test, along with the measurement amplitude time history.

## 4.6.5.1 Controls.

Test levels for this test are shown in Table 516.6-VI. Test the item in the same configuration that is used in a transportation, handling, or a combat situation. For test items under 45 kg (100 pounds), the 26-drop requirement (Table 516.6-VI) may be divided among up to five samples of the same test item in any combination. Toppling of the item following impact will occur in the field and, therefore, toppling of the test item following its initial impact should not be restrained as long as the test item does not leave the required drop surface. Levels for this test were set by considering how materiel in the field might commonly be dropped. (For example, a light item might be carried by one man, chest high; thus it could drop 122 cm (48 inches).) Field data have shown that a typical piece of man-portable materiel will be dropped from heights up to 122 cm an average of four to six times during its life cycle. The 26-drop requirement exists to ensure each vulnerable position (faces, edges, and corners) of a typical test item receives an impact. Conduct drops for equipment up to 454 kg (1000 pounds) and having its largest dimension

less than 91 cm (36 inches) using a quick release hook, or drop tester. For the floor or barrier receiving the impact, use two-inch plywood backed by concrete. For materiel over 454 kg, use a concrete floor or barrier.

Weight of Test Item & Case kg (lbs)	Largest Dimension, cm (in)	Notes	Height of Drop, h cm (in)	Number of Drops
Under 45.4 (100) Manpacked or man-portable	Under 91 (36)	<u>A/</u>	122 (48)	Drop on each face, edge and corner; total of 26 drops <u>D</u> /
1	91 & over	A/	76 (30)	
45.4 - 90.8 (100 - 200) inclusive	Under 91	<u>A/</u>	76 (30)	Drop on each corner; total of eight drops
	91 & over	<u>A/</u>	61 (24)	
90.8-454 (200 – 1000) inclusive	Under 91	<u>A/</u>	61 (24)	
	91 – 152 (36 – 60)	<u>B/</u>	61 (24)	
	Over 152	<u>B/</u>	61 (24)	
Over 454	No limit	<u>C/</u>	46 (18)	Drop on each bottom edge. Drop on bottom face or skids; total of five drops

## Table 516.6-VI. Transit drop test.

## NOTES:

 $\underline{A}$ / Perform drops from a quick-release hook or drop tester. Orient the test item so that, upon impact, a line from the struck corner or edge to the center of gravity of the case and contents is perpendicular to the impact surface.

 $\underline{B}$ / With the longest dimension parallel to the floor, support the transit, or combination case with the test item within, at the corner of one end by a block 13 cm (five inches) in height, and at the other corner or edge of the same end by a block 30 cm (12 inches) in height. Raise the opposite end of the case to the specified height at the lowest unsupported corner and allow it to fall freely.

 $\underline{C}$ / While in the normal transit position, subject the case and contents to the edgewise drop test as follows (if the normal transit position is unknown, orient the case so the two longest dimensions are parallel to the floor):

Edgewise drop test: Support one edge of the base of the case on a sill 13-15 cm (five to six inches) in height. Raise the opposite edge to the specified height and allow it to fall freely. Apply the test once to each edge of the base of the case (total of four drops).

 $\underline{D}$ / If desired, divide the 26 drops among no more than five test items (see paragraph 4.6.5.1).

## 4.6.5.2 Test tolerances.

Ensure the test height of drop is within 2.5 percent of the height of drop as specified in Table 516.6-VI.

# 4.6.5.3 Procedure IV – Transit Drop.

- Step 1. After performing a visual inspection and operational check for baseline data, install the test item in its transit or combination case as prepared for field use (if measurement information is to be obtained, install and calibrate such instrumentation in this Step). If the test item operates satisfactorily, proceed to Step 2. If not, resolve the problems and repeat this step.
- Step 2. From paragraph 4.6.5.1 and Table 516.6-VI, determine the height of the drops to be performed, the number of drops per test item, and the drop surface.
- Step 3. Perform the required drops using the apparatus and requirements of paragraphs 4.6.5 and 4.6.5.1 and Table 516.6-VI notes. Recommend visually and/or operationally checking the test item periodically

during the drop test to simplify any follow-on evaluation that may be required. If any degradation is noted, see paragraph 4.3.2.

- Step 4. Document the impact point or surface for each drop and any obvious damage.
- Step 5. Following completion of the required drops, visually examine the test item(s), and document the results.
- Step 6. Conduct an operational checkout in accordance with the approved test plan. See paragraph 5 for analysis of results.
- Step 7. Document the results for comparison with data obtained in Step 1, above.

#### 4.6.6 Procedure V - Crash Hazard Shock Test.

The intent of this procedure is to disclose structural failures of materiel or mounts for materiel in air or ground vehicles that may present a hazard to personnel or other materiel if the materiel breaks loose from its mount during or after a vehicle crash. This test procedure is intended to verify that materiel mounting and/or restraining devices will not fail, and that sub-elements are not ejected during crash situations. Attach the test item to its shock fixture by its in-service mounting or tiedowns.

#### 4.6.6.1 Controls.

Use Figure 516.6-8 as the test spectrum for the axis of test with the effective shock duration,  $T_e$ , between 15 and 23 milliseconds for flight materiel, and between 8 and 13 milliseconds for ground materiel. If shock spectrum analysis capabilities are not available, the classical terminal peak sawtooth pulse in Figure 516.6-10 may be used as an alternative to a complex transient waveform developed from the SRS in Figure 516.6-8. Table 516.6-VII provides the parameters for the terminal peak sawtooth pulse. An aircraft crash level of 40 gs is based on the assumption that, during a survivable crash, localized g levels can approach 40 g's. Ground transportation vehicles are designed with a higher safety factor and, therefore, must sustain a much higher g level with correspondingly higher specified test levels.

	Minimum (A <sub>m</sub>	Peak Value ) g's	Nominal Dur	ation (T <sub>D</sub> ) ms
Test	Flight Vehicle Equipment <sup>1/</sup> a	Ground Equipment b	Flight Vehicle Equipment <sup>1/</sup> c	Ground Equipment d
Crash Hazard Shock Test	40	75	11	6

#### Table 516.6-VII. Terminal peak sawtooth pulse test parameters (refer to Figure 516.6-10).

<sup>1/2</sup> Shock parameters a and c: Recommend for materiel not shock-mounted and weighing less than 136 kg (300 lbs).</sup>

## 4.6.6.2 Test tolerances.

For complex waveform replication based upon SRS, ensure the test tolerances are within those specified for the SRS in paragraph 4.2.2. For the classical pulse terminal peak sawtooth pulse described in Table 516.6-VII, ensure the waveform is within the tolerances specified in Figure 516.6-10.

## 4.6.6.3 Procedure V – Crash Hazard Shock Test.

- Step 1. Secure the test item mount to the shock apparatus by its in-service mounting configuration. Use a test item that is dynamically similar to the materiel, or a mechanically equivalent mockup. If a mockup is used, it will represent the same hazard potential, mass, center of mass, and mass moments about the attachment points as the materiel being simulated. (If measurement information is to be collected, mount and calibrate the instrumentation.)
- Step 2. Perform two shocks in each direction (as determined in paragraph 2.3.3) along three orthogonal axes of the test item for a maximum of 12 shocks.
- Step 3. Perform a physical inspection of the test setup. Operation of the test item is not required.
- Step 4. Document the results of the physical inspection, including an assessment of potential hazards created by either materiel breakage or structural deformation, or both. Process any measurement data according to the maximax acceleration SRS or the pseudovelocity SRS.

## 4.6.7 Procedure VI - Bench handling.

The intent of this test is to determine the ability of materiel to withstand the usual level of shock associated with typical bench maintenance or repair. Use this test for any materiel that may experience bench or bench-type maintenance. This test considers both the structural and functional integrity of the materiel.

#### 4.6.7.1 Controls.

Ensure the test item is a fully functional representative of the materiel. Raise the test item at one edge 100 mm (4 in) above a solid wooden bench top or until the chassis forms an angle of  $45^{\circ}$  with the bench top or until point of balance is reached, whichever is less. (The bench top must be at least 4.25 cm (1.675 inches) thick.) Perform a series of drops in accordance with specifications. The heights used during this test are defined by examining the typical drops that are commonly made by bench technicians and assembly line personnel.

## 4.6.7.2 Test tolerances.

Ensure the test height of drop is within 2.5 percent of the height of drop as specified in paragraph 4.5.7.1.

## 4.6.7.3 Procedure VI – Bench Handling.

- Step 1. Following an operational and physical checkout, configure the item as it would be for servicing, e.g., with the chassis and front panel assembly removed from its enclosure. If the test item operates satisfactorily, proceed to Step 2. If not, resolve the problems and repeat this Step. Position the test item as it would be for servicing. Generally, the test item will be non-operational during the test.
- Step 2. Using one edge as a pivot, lift the opposite edge of the chassis until one of the following conditions occurs (whichever occurs first).
  - a. The lifted edge of the chassis has been raised 100 mm (4 in) above the horizontal bench top.
  - b. The chassis forms an angle of  $45^{\circ}$  with the horizontal bench top.
  - c. The lifted edge of the chassis is just below the point of perfect balance. Let the chassis drop back freely to the horizontal bench top. Repeat using other practical edges of the same horizontal face as pivot points, for a total of four drops.
- Step 3. Repeat Step 2 with the test item resting on other faces until it has been dropped for a total of four times on each face on which the test item could be placed practically during servicing.
- Step 4. Visually inspect the test item.
- Step 5. Document the results.
- Step 6. Operate the test item in accordance with the approved test plan. See paragraph 5 for analysis of results.
- Step 7. Document the results for comparison with data obtained in Step 1, above.

## 4.6.8 Procedure VII - Pendulum Impact

## 4.6.8.1 Controls.

a. The pendulum impact tester consists of a platform suspended from a height at least 5m above the floor by four or more ropes, chains, or cables; and a bumper comprised of a flat, rigid concrete or masonry wall, or other equally unyielding flat barrier. The bumper is at least 46cm (18.1 in) high; wide enough to make full contact with the container end, and has sufficient mass to resist the impacts without displacement. The impact surface is oriented perpendicular to the line of swing of the platform. The platform is large enough to support the container or pack, and when hanging free, has its top surface approximately 23cm (9.1 in) above the floor, and its leading edge at least 8cm (3.1 in) from the surface of the bumper. The suspension chains are vertical and parallel so that when the platform is pulled straight back, it will rise uniformly but remain at all times horizontal and parallel to the floor (see Figure 516.6-13).



Figure 516.6-13. Pendulum impact test.

- b. The test item (large shipping container) may consist of a box, case, crate or other container constructed of wood, metal, or other material, or any combination of these for which ordinary box tests are not considered practical or adequate. Unless otherwise specified, large containers are those that measure more than 152cm (60 in) on any edge or diameter, or those when loaded have gross weights in excess of 70kg (154 lbs).
- c. Load the test item (container) with the interior packing and the actual contents for which it was designed. If use of the actual contents is not practical, a dummy load may be substituted to simulate such contents in weight, shape, and position in the container. Block and brace the contents, or dummy load, and cushion them in place as for shipment. When the pendulum impact test is performed to evaluate the protection provided for the contents, the rigidity of a dummy load should closely approximate that of the actual contents for which the pack was designed.

## 4.6.8.2 Test tolerances.

Ensure the vertical drop height is within 2.5 percent of the required height.

## 4.6.8.3 Procedure VII – Pendulum Impact.

- Step 1. If required, perform a pretest operational checkout in accordance with the test plan. Install accelerometers and other sensors on the test item, as required.
- Step 2. Place the test item on the platform with the surface that is to be impacted projecting beyond the front end of the platform so that the specimen just touches the vertical surface of the bumper.
- Step 3. Pull back the platform so that the center of gravity of the pack is raised to the prescribed height, and then release it to swing freely so that the surface of the container impacts against the bumper.

Unless otherwise specified, the vertical height is a drop of 23cm (9 in) that results in a velocity of 214cm/sec (7 ft/sec) at impact.

- Step 4. Examine the test item and record obvious damage. If the container is undamaged, rotate it 180 degrees and repeat Step 3. When the test is conducted to determine satisfactory performance of a container or pack, and unless otherwise specified, subject each test item to one impact to each side and each end that has a horizontal dimension of less than 3m (9.8 ft).
- Step 5. Record any changes or breaks in the container, such as apparent racking, nail pull, or broken parts, and their locations. Carefully examine the packing (blocks, braces, cushions, or other devices) and the contents, and record their condition. If required, perform a post test operational checkout in accordance with the test plan. See paragraph 5 for analysis of results.

## 4.6.9 Procedure VIII - Catapult Launch/Arrested Landing.

The intent of this test is to verify the functionality and structural integrity of materiel mounted in or on fixed wing aircraft that are subject to catapult launches and arrested landings.

## 4.6.9.1 Controls.

- a. Measured data not available. Whenever possible, derive the test conditions from measured data on applicable carrying aircraft (see Part One, paragraph 5.6, as well as the tasks at the end of Part One in Annex A for information on the use of field/fleet data), since shock responses can be affected by local influences such as wing and fuselage bending modes, pylon interfaces, and structural damping. While the pulse amplitudes associated with this environment are generally low, the long periods of application and high frequency of occurrence have the potential to cause significant dynamic and/or low cycle fatigue damage in improperly designed materiel. A typical aircraft may fly as many as 200 sorties per year, of which more than two-thirds involve catapult launches and arrested landings. However, for laboratory test purposes, 30 simulated catapult/arrested landing events in each of two axes (longitudinal and vertical) should provide confidence that the majority of significant defects will be identified for remedial action. If acceptable field-measured data are not available, the following guidance is offered in which sinusoidal burst is used to simulate each catapult or launch event. This time history has been simplified to a constant amplitude sine burst of 2-second duration for simulation. In paragraph 4.6.9.1a(5), measured data seem to indicate that response in the horizontal direction can be comparable to that in the vertical direction. For testing purposes, it is permissible to reduce the maximum amplitude in the horizontal direction to 75 percent of that in the vertical direction.
  - (1) Wave shape: damped sine wave.
  - (2) Wave frequency: determined by structural analysis of the specific aircraft and frequency of the fundamental mode.
  - (3) Burst amplitude: determined by structural analysis of the specific aircraft, the frequency of the fundamental mode and the location of the materiel relative to the shape of the fundamental mode.
  - (4) Wave damping (quality factor): Q = 20.
  - (5) Axis: vertical, horizontal, longitudinal.
  - (6) Number of bursts: determined by the specific application (for example, 30 bursts, each followed by a 10 second rest period).
- b. <u>Measured data available</u>. If acceptable field measured data are available, the following guidance is offered in which the catapult event is simulated by two shocks separated by a transient vibration, and the arrested landing event by one shock followed by transient vibration. The catapult launch/arrested landing shock environment differs from other typical shock events in that it is a transient periodic vibration (roughly sinusoidal) at a relatively low frequency determined by aircraft mass and landing gear damping characteristics. Typical catapult launch shock time histories are shown on Figure 516.6-14. These data represent measured acceleration response in the vertical, horizontal and longitudinal directions of a store component mounted on the pylon of a platform. The data are DC coupled and lowpass filtered at 70 Hz. All three time histories demonstrate an initial transient, followed by a transient vibration (nearly two seconds long), and concluded by a final transient. The longitudinal axis provides a profile of the DC catapult acceleration that, in general, will not be important for testing purposes and can be removed by high pass filtering the time history at a frequency less than 10 percent of the lowest significant frequency in the maximax acceleration SRS. Procedures for accomplishing this filtering may necessarily be iterative (unless Fourier transform information is used) with high pass

filtering beginning at a comparatively high frequency and decreasing until the most significant SRS low frequency is identified. In general, catapult acceleration response will display two shock events corresponding to initial catapult load application to the aircraft and catapult release from the aircraft separated by an oscillatory acceleration. Both the initial and the final shock events have a distinct oscillatory nature. It is essential that this test be run as a series of two shock transients separated by a two second period of time in which transient vibration may be input. Typical arrested landing shock time histories are shown on Figure 516.6-15. These data represent measured acceleration response in the vertical, horizontal and longitudinal directions of a store component mounted on the pylon of a platform. The data are DC coupled and low pass filtered at 70 Hz. All three time histories demonstrate an initial transient, followed by a transient vibration (nearly three seconds long). It is clear that the longitudinal time history has a comparatively large DC component that may be filtered out for test specification development. The term "transient vibration" is introduced here because of the duration of the event being not typical of a shock event.

**Note**: <u>Transient vibrations</u>. For precise laboratory simulation, Procedure VIII may require consideration of the concept of a transient vibration in processing and replication of the form of time history from measured data. For long duration transient environments (durations on the order of one second or more), it may be useful to process the response time history by estimating the envelope function, a(t), and proceeding to compute a maximax Autospectral Density Estimate (ASD), assuming short portions of the response time history processing and will not be considered further in this method</u>. For a precise definition of transient vibration see Part One, Annex D. The importance of the transient vibration phenomenon is that (1) it has the form of a shock (short duration and substantial time varying amplitude), (2) it can be mathematically modeled in a precise way, and (3) it can be used in stochastic simulation of certain shock environments. In general, shocks have their significant energy in a shorter time frame than transient vibrations, while transient vibrations allow for time history enveloping functions other than the exponential envelope form often times displayed in shocks as a result of resonant response decay to an impact.



Figure 516.6-14. Sample measured store three axis catapult launch component response acceleration time histories.

## 4.6.9.2 Test tolerances.

For cases in which measured data are not available and waveforms are generated from dynamic analysis of the configuration, ensure the waveform tolerances are within the time history test tolerances specified for waveforms in paragraph 4.2.2. For cases in which measured data are available, ensure the SRS for the test response is within the SRS tolerances specified in paragraph 4.2.2. For transient vibration, ensure the waveform peaks and valleys are within the tolerances given for waveforms in paragraph 4.2.2 or as provided in the test specification.

## 4.6.9.3 Procedure VIII - Catapult Launch/Arrested Landing.

- Step 1. Mount the test item to its shock/vibration fixture on the shock device for the first test axis.
- Step 2. Attach instrumentation as required in the approved test plan.
- Step 3. Conduct an operational checkout and visual examination in accordance with the approved test plan. If the test item operates satisfactorily, proceed to Step 4. If not, resolve the problems and repeat this step.
- Step 4. a. If no measured field data are available, apply short transient sine waves of several cycles to the test item in the first test axis. (Each short transient sine wave of several cycles represents a single catapult or arrested landing event.) Follow each burst by a rest period to prevent unrepresentative effects. Operate the test item in its appropriate operational mode while bursts are applied. If the test item fails to operate as intended, follow the guidance in paragraph 4.3.2 for test item failure.
  - b. If measured field data are available, either apply the measured response data under exciter system wave form control (see Method 519.6, Annex A), or process the catapult as two shocks separated by a transient vibration, and the arrested landing as a shock followed by a transient vibration.
- Step 5. If the test item has not malfunctioned during testing, conduct an operational checkout and visual examination in accordance with the approved test plan. If a failure has occurred, it may be desirable to perform a thorough visual examination before proceeding with the operational checkout to avoid

initiating additional hardware damage. When a failure occurs, consider the nature of the failure and corrective action along with the purpose of the test (engineering information or contractual compliance) in determining whether to restart the test or to continue from the point of interruption. If the test item does not operate satisfactorily, follow the guidance in paragraph 4.3.2 for test item failure.

Step 6. Repeat Steps 1 through 5 for the second test axis.

Step 7. Document the test results including amplitude time history plots, and notes of any test item operational or structural degradation. See paragraph 5 for analysis of results.

## 5. ANALYSIS OF RESULTS.

In addition to the specific guidance provided in the test plan and the general guidance provided in Part One, paragraphs 5.14 and 5.17, and Part One, Annex A, Task 406, refer to the below paragraphs for supplemental test analysis information. Analyze any failure of a test item to meet the requirements of the materiel specifications.

- a. Procedure I (Functional Shock) Consider any interruption of the materiel operation during or after the shock in relationship to the materiel's operational test requirements. (See paragraph 4.3.2.)
- b. Procedure II (Materiel to be Packaged).-.Consider any damage to the shock mounts or the internal structural configuration of the test item that may provide a cause for the development of a failure analysis course of action to consider retrofit or redesign.
- c. Procedure III (Fragility) The outcome of a successful fragility test is one specified measurement level of test item failure for each test axis. Consider that if the test item fails either operationally or structurally at the lowest level of testing, and there is no provision for testing at lower levels, the test item's fragility level is indeterminate.
- d. Procedure IV (Transit Drop) In general, analysis of results will consist of visual and operational comparisons for before and after test. Measurement instrumentation and subsequent processing of acceleration time history information can provide valuable information related to response characteristics of the test item and statistical variation in the shock environment.
- e. Procedure V (Crash Hazard Shock Test) If measurement information was obtained, process this in accordance with paragraph 4.6.6.3, Step 4.
- f. Procedure VI (Bench Handling) In general, any operational or physical (mechanical or structural) change of configuration from Step 1 in paragraph 4.6.7.3 must be recorded and analyzed.
- g. Procedure VII (Pendulum Impact) In general, analysis of the results will consist of visual inspections and any operational comparisons before and after the test. Check for operability and inspect for physical damage of the contents (except when using a dummy load). Damage to the exterior shipping container that is the result of improper interior packaging, blocking, or bracing is cause for rejection. Structural damage to the exterior shipping container that results in either spilling of the contents or failure of the container in subsequent handling is cause for rejection. Assess whether a substantial amount of shifting of the contents within the shipping container created conditions likely to cause damage during shipment, storage, and reshipment of the container. Minor container damage such as chipping of wood members, dents, paint chipping, is not cause for rejection. If recorded, acceleration time histories or other sensor data can provide valuable information related to the response characteristics of the test item.
- h. Procedure VIII (Catapult Launch/Arrested Landing) Consider any failure of the structural configuration of the test item, mount, or launcher that may not directly impact failure of the operation of the materiel, but that would lead to failure under in-service conditions.

## 6. REFERENCE/RELATED DOCUMENTS.

## 6.1 Referenced Documents.

- Handbook for Dynamic Data Acquisition and Analysis, IES-RP-DTE012.2, Institute of Environmental Sciences and Technology, Arlington Place One, 2340 S. Arlington Heights Road, Suite 100, Arlington Heights, IL 60005-4516; <u>Institute of Environmental Sciences and Technology</u>.
- b. Piersol, Allan G., Determination of Maximum Structural Responses From Predictions or Measurements at Selected Points, Proceedings of the 65th Shock and Vibration Symposium, Volume I, SAVIAC, 1994. Shock & Vibration Information Analysis Center (SAVIAC), Three Chopt Rd. (Suite 110), Richmond, VA 23229.
- c. MIL-S-901, "Shock Tests, H.I. (High Impact), Shipboard Machinery, Equipment and Systems, Requirements for."
- d. MIL-STD-331, Fuze and Fuze Components, Environmental and Performance Tests for.
- e. Gaberson, H. A. and R. H. Chalmers. Model Velocity as a Criterion of Shock Severity, Shock and Vibration Bulletin 40, Pt. 2, 1969, pp.31-49.
- f. Harris, C., and C. E. Crede, eds., Shock and Vibration Handbook, 5th Edition, NY, McGraw-Hill.
- g. ANSI/ASTM D3332, Standard Test Methods for Mechanical-Shock Fragility of Products, Using Shock Machines; <u>Information Handling Services</u>.
- h. AR 70-44, DoD Engineering for Transportability; Information Handling Services.
- i. Fackler, Warren C, "Equivalence Techniques for Vibration Testing", SVM-9, The Shock Vibration Information Center, Naval Research Laboratory, Washington D.C., 1972.
- j. Miles, J., :On Structural Fatugue Under Random Loading,". J. Aeronaut. Sci. 21, 753-762, November 1954.

## 6.2 Related Documents.

- a. Conover, W.J., Practical Nonparametric Statistics. New York; Wiley, 1971, Chapter 3.
- b. Piersol, A.G., Analysis of Harpoon Missile Structural Response to Aircraft Launches, Landings and Captive Flight and Gunfire. Naval Weapons Center Report #NWC TP 58890. January 1977.
- c. Bendat, J. S. and A. G. Piersol, Random Data: Analysis and Measurement Procedures, John Wiley & Sons Inc., New York, 1986
- d. Schock, R. W. and W. E. Paulson, TRANSPORTATION A Survey of Shock and Vibration Environments in the Four Major Modes of Transportation, Shock and Vibration Bulletin #35, Part 5, February 1966.
- e. Ostrem, F. E., TRANSPORTATION AND PACKAGING A Survey of the Transportation Shock and Vibration Input to Cargo, Shock and Vibration Bulletin #42, Part 1, January 1972. Shock & Vibration Information Analysis Center (SAVIAC), Three Chopt Rd. (Suite 110), Richmond, VA 23229.
- f. Allied Environmental Conditions and Test Procedure (AECTP) 400, Mechanical Environmental Tests (under STANAG 4370), Methods 403, 416, and 417.
- g. MIL-STD-209K, Lifting and Tiedown Provisions.
- h. DOD Directive 4510.11, DOD Transportation Engineering.
- i. Egbert, Herbert W. "The History and Rationale of MIL-STD-810," February 2005; Institute of Environmental Sciences and Technology, Arlington Place One, 2340 S. Arlington Heights Road, Suite 100, Arlington Heights, IL 60005-4516.

(Copies of Department of Defense Specifications, Standards, and Handbooks, and International Standardization Agreements are available online at <u>http://assist.daps.dla.mil/quicksearch/</u> or from the Standardization Document Order Desk, 700 Robbins Avenue, Building 4D, Philadelphia, PA 19111-5094.)

Requests for other defense-related technical publications may be directed to the Defense Technical Information Center (DTIC), ATTN: DTIC-BR, Suite 0944, 8725 John J. Kingman Road, Fort Belvoir VA 22060-6218, 1-800-225-3842 (Assistance--selection 3, option 2), <u>http://stinet.dtic.mil/info/s-stinet.html</u>; and the National Technical Information Service (NTIS), Springfield VA 22161, 1-800-553-NTIS (6847), <u>http://www.ntis.gov/</u>.

## **METHOD 516.6 ANNEX A**

## Statistical Considerations for Developing Limits on Predicted and Processed Data

#### 1. SCOPE.

#### 1.1 Purpose.

This Annex provides information relative to the statistical characterization of a set of data for the purpose of defining an upper limit of the data set related to statistical/probabilistic considerations.

#### 1.2 Application.

Information in this Annex is generally applicable to frequency domain estimates that are either predicted based on given information or time domain measurements processed in the frequency domain according to an appropriate technique i.e., for stationary random vibration, the processing would be an ASD; for a very short transient the processing could be an SRS, ESD, or FS. Given estimates in the frequency domain, information in this Annex will allow the establishment of upper limits of the data in a statistically correct way. Statistically based lower limits may be established on a data set for positive amplitude e.g., ASD estimates, by inverting the amplitudes and proceeding as in the case of establishment of upper limits, subsequently inverting the resulting 'upper limit' for the desired statistically based lower limit. When using a dB representation of amplitude the process of inversion represents a change in sign for the amplitude and subsequent application of the 'upper limit' procedure that with sign reversal results in the desired statistically based lower limit.

#### 2. DEVELOPMENT.

#### 2.1 Basic Estimate Assumptions.

Prediction estimates, measurement estimates, or a combination of prediction and measurement estimates may be considered in the same manner. It is assumed that uncertainty in individual measurements (processing error) does not effect the limit considerations. For measured field data digitally processed such that estimates of the SRS, ESD, FS, or ASD are obtained for single sample records, it is useful to examine and summarize the overall statistics of "similar" estimates selected in a way so as to not bias the summary statistics. To ensure the estimates are not biased, the measurement locations might be chosen randomly, consistent with the measurement objectives. Similar estimates may be defined as (1) estimates at a single location on materiel that has been obtained from repeated testing under essentially identical experimental conditions; (2) estimates on a system that have been obtained from one test, where the estimates are taken (a) at several neighboring locations; or (3) some combination of (1) and (2). In any case, it is assumed that there is a certain degree of homogeneity among the estimates across the frequency band of interest. This latter assumption generally requires that (1) the set of estimates for a given frequency have no significant "outliers" that can cause large sample variance estimates, and (2) larger input stimulus to the system from which the measurements are taken implies larger estimate values.

#### 2.2 Basic Estimate Summary Preprocessing.

There are two ways in which summaries may be obtained. The first way is to use an "enveloping" scheme on the basic estimates to arrive at a conservative estimate of the environment, and some qualitative estimate of the spread of basic estimates relative to this envelope. This procedure is dependent upon the judgment of the analyst and, in general, does not provide consistent results among analysts. The second way is to combine the basic estimates in some statistically appropriate way and infer the statistical significance of the estimates based upon probability distribution theory. Paragraph 6.1, reference b summarizes the current state of knowledge relative to this approach and its relationship to determining upper limits on sets of data. In general, the estimates referred to and their statistics are related to the same frequency band over which the processing takes place. Unfortunately, for a given frequency band, the statistics behind the overall set of estimates are not easily accessible because of the unknown distribution function of amplitudes for the frequency band of interest. In most cases the distribution function can be assumed to be normal, provided the individual estimates are transformed to a "normalizing" form by computing the logarithm to the base ten of the estimates. For ESD and FS estimates, the averaging of adjacent components (assumed to be statistically independent) increases the number of degrees of freedom in the estimates. For ASD estimates, averaging of adjacent components can be useful provided the bias error in the estimate is small; i.e., the

resolution filter bandwidth is a very small fraction of the overall estimate bandwidth. For SRS estimates, because they are based on maximum response of a single-degree-of-freedom system as its natural frequency is varied, adjacent estimates tend to be statistically dependent and, therefore, not well smoothed by averaging unless the SRS is computed for very narrow frequency spacing. In such cases, smoothing of SRS estimates is better accomplished by reprocessing the original time history data at a broader natural frequency spacing, e.g., 1/6th octave as opposed to 1/12th octave. There is no apparent way to smooth dependent SRS estimates mathematically when reprocessing cannot be performed, and the acceptable alternative is some form of enveloping of the estimates. The larger the sample size, the closer the logarithm transform of the estimates is to the normal distribution unless there is a measurement selection bias error in the experiment. Finally, generally, before application, the upper limits obtained in the paragraphs to follow are smoothed by straight line segments intersecting at spectrum "breakpoints." No guidance is provided in this Annex relative to this "smoothing" or "enveloping" procedure, e.g., whether estimates should be clipped or enveloped and the relationship of the bandwidth of the estimates to the degree of clipping, etc., except that such smoothing should be performed only by an experienced analyst. Paragraph 6.1, reference b discusses this further.

#### 2.3 Parametric Upper Limit Statistical Estimate Assumptions.

In all the formulas for the estimate of the statistical upper limit of a set of N predictions or measurements,

$$\{x_1, x_2, \dots, x_N\},\$$

it is assumed that (1) the estimates will be logarithm transformed to bring the overall set of measurements closer to those sampled of a normal distribution and (2) the measurement selection bias error is negligible. Since the normal and "t" distribution are symmetric, the formulas below apply for the lower bound by changing the sign between the mean and the standard deviation quantity to minus. It is assumed here that all estimates are at a single frequency or for a single bandwidth, and that estimates among bandwidths are independent so that each bandwidth under consideration may be processed individually, and the results summarized on one plot over the entire bandwidth as a function of frequency. For

$$y_i = \log_{10}(x_i)$$
  $i = 1, 2, ..., N$ 

Mean estimate for true mean,  $\mu_v$  is given by

$$m_y = \frac{1}{N} \sum_{i=1}^{N} y_i$$

and the unbiased estimate of the standard deviation for the true standard deviation  $\sigma_v$  is given by

$$s_{y} = \sqrt{\frac{\sum\limits_{i=1}^{N} (y_{i} - m_{y})^{2}}{N-1}}$$

## 2.3.1 NTL - Upper normal one-sided tolerance limit.

The upper normal one-sided tolerance limit on the proportion  $\beta$  of population values that will be exceeded with a confidence coefficient,  $\gamma$ , is given by NTL(N,  $\beta$ ,  $\gamma$ ), where

$$NTL(N,\beta,\gamma) = 10^{m_y + s_y k_{N,\beta,\gamma}}$$

where  $k_{N,\beta,\gamma}$  is the one-sided normal tolerance factor given in Table 516.6A-I for selected values of N,  $\beta$  and  $\gamma$ . NTL is termed the upper one-sided normal tolerance interval (of the original set of estimates) for which 100  $\beta$  percent of the values will lie below the limit with 100  $\gamma$  percent confidence. For  $\beta = 0.95$  and  $\gamma = 0.50$ , this is referred to as the 95/50 limit.

The following table from paragraph 6.1, reference b, contains the k value for selected N,  $\beta$ ,  $\gamma$ . In general this method of estimation should not be used for small N with values of  $\beta$  and  $\gamma$  close to 1 since it is likely the assumption of the normality of the logarithm transform of the estimates will be violated.

N		$\gamma = 0.50$			$\gamma = 0.90$			$\gamma = 0.95$	
N	β = 0.90	β = 0.95	β = 0.99	β = 0.90	β = 0.95	β = 0.99	β = 0.90	$\beta = 0.95$	β = 0.99
3	1.50	1.94	2.76	4.26	5.31	7.34	6.16	7.66	10.55
4	1.42	1.83	2.60	3.19	3.96	5.44	4.16	5.14	7.04
5	1.38	1.78	2.53	2.74	3.40	4.67	3.41	4.20	5.74
6	1.36	1.75	2.48	2.49	3.09	4.24	3.01	3.71	5.06
7	1.35	1.73	2.46	2.33	2.89	3.97	2.76	3.40	4.64
8	1.34	1.72	2.44	2.22	2.76	3.78	2.58	3.19	4.35
9	1.33	1.71	2.42	2.13	2.65	3.64	2.45	3.03	4.14
10	1.32	1.70	2.41	2.06	2.57	3.53	2.36	2.91	3.98
12	1.32	1.69	2.40	1.97	2.45	3.37	2.21	2.74	3.75
14	1.31	1.68	2.39	1.90	2.36	3.26	2.11	2.61	3.58
16	1.31	1.68	2.38	1.84	2.30	3.17	2.03	2.52	3.46
18	1.30	1.67	2.37	1.80	2.25	3.11	1.97	2.45	3.37
20	1.30	1.67	2.37	1.76	2.21	3.05	1.93	2.40	3.30
25	1.30	1.67	2.36	1.70	2.13	2.95	1.84	2.29	3.16
30	1.29	1.66	2.35	1.66	2.08	2.88	1.78	2.22	3.06
35	1.29	1.66	2.35	1.62	2.04	2.83	1.73	2.17	2.99
40	1.29	1.66	2.35	1.60	2.01	2.79	1.70	2.13	2.94
50	1.29	1.65	2.34	1.56	1.96	2.74	1.65	2.06	2.86
$\infty$	1.28	1.64	2.33	1.28	1.64	2.33	1.28	1.64	2.33

Table 516.6A-I. Normal tolerance factors for upper tolerance limit.

## 2.3.2 NPL - Upper normal prediction limit.

The upper normal prediction limit is the value of x (for the original data set) that will exceed the next predicted or measured value with confidence coefficient,  $\gamma$ , and is given by

$$m_{y} + s_{y}\sqrt{1 + \frac{1}{N}} t_{N-1;\alpha}$$
NPL(N,  $\gamma$ ) = 10

where  $\alpha = 1 - \gamma$ .  $t_{N-1; \alpha}$  is the student t distribution variable with N-1 degrees of freedom at the 100  $\alpha = 100(1-\gamma)$  percentage point of the distribution. This estimate, because of the assumptions behind its derivation, requires careful interpretation relative to measurements made in a given location or over a given zone (paragraph 6.1, reference b).

#### 2.4 Nonparametric Upper Limit Statistical Estimate Assumptions.

If there is some reason to believe that the data, after it has been logarithm-transformed, will not be sufficiently normally distributed to apply the parametric limits defined above, consideration must be given to nonparametric limits, i.e., limits that are not dependent upon assumptions concerning the distribution of estimate values. In this case there is no need to transform the data estimates. All of the assumptions concerning the selection of estimates are applicable for nonparametric estimates. With additional manipulation, lower bound limits may be computed.

#### **2.4.1** ENV – Upper limit.

The maximum upper limit is determined by selecting the maximum estimate value in the data set.

$$ENV(N) = max \{ x_1, x_2, \dots, x_N \},.$$

The main disadvantage of this estimate is that the distributional properties of the estimate set are neglected so that no probability of exceedance of this value is specified. In the case of outliers in the estimate set, ENV(N) may be far too conservative. ENV(N) is also sensitive to the bandwidth of the estimates.

#### 2.4.2 DFL – Upper distribution-free tolerance limit.

The distribution-free tolerance limit that uses the original untransformed sample values is defined to be the upper limit for which at least the fraction  $\beta$  of all sample values will be less than the maximum predicted or measured value with a confidence coefficient of " $\gamma$ ." This limit is based on order statistic considerations.

$$DFL(N,\beta,\gamma) = x_{max}; \gamma = 1-\beta^{N}$$

where  $x_{max}$  is the maximum value of the set of estimates,  $\beta$ , is the fractional proportion below  $x_{max}$ , and  $\gamma$  is the confidence coefficient. N,  $\beta$  and  $\gamma$  are not independently selectable. That is

- (1) Given N and assuming a value of  $\beta$ ,  $0 \le \beta \le 1$ , the confidence coefficient can be determined.
- (2) Given N and  $\gamma$ , the proportion  $\beta$  can be determined.
- (3) Given  $\beta$  and  $\gamma$ , the number of samples can be determined such that the proportion and confidence can be satisfied (for statistical experiment design).

DFL(N, $\beta$ , $\gamma$ ) may not be meaningful for small samples of data, N  $\leq$  13, and comparatively large  $\beta$ ,  $\beta$  > 0.95. DFL(N, $\beta$ , $\gamma$ ) is sensitive to the estimate bandwidth.

#### 2.4.3 ETL – Upper empirical tolerance limit.

The empirical tolerance limit uses the original sample values and assumes the predicted or measured estimate set is composed of N measurement points over M frequency resolution bandwidths for a total of NM estimate values. That is

 $\{x_{11}, x_{12}, \dots, x_{1M}; x_{21}, x_{22}, \dots, x_{2M}; x_{N1}, x_{N2}, \dots, x_{NM}\}$ 

where m<sub>i</sub> is the average estimate at the jth frequency bandwidth over all N measurement points

$$m_{j} = \frac{1}{N} \sum_{i=1}^{N} x_{ij}$$
  $j = 1, 2, ..., M$ 

mi is used to construct an estimate set normalized over individual frequency resolution bandwidths. That is

 $\{u\} = \{u_{11}, u_{12}, \dots, u_{1M}, u_{21}, u_{22}, \dots, u_{2M}, u_{N1}, u_{N2}, \dots, u_{NM}\}$ 

where : 
$$u_{ij} = \frac{x_{ij}}{m_j}$$
  $i = 1, 2, ..., N; j = 1, 2, ..., M$ 

The normalized estimate set, {u}, is ordered from smallest to largest and

 $u_{\beta} = u_{(k)}$  where  $u_{(k)}$  is the k<sup>th</sup> ordered element of set  $\{u\}$  for  $0 \le \beta = \frac{k}{MN} \le 1$ 

is defined. For each resolution frequency bandwidth, then

$$ETL(\beta) = u_{\beta}m_{j} = x_{\beta j}$$
  $j = 1, 2, ..., M$ 

Using  $m_j$  implies that the value of ETL( $\beta$ ) at j exceeds  $\beta$  percent of the values with 50 percent confidence. If a value other than  $m_j$  is selected, the confidence level may increase. It is important that the set of estimates is homogeneous to use this limit, i.e., they have about the same spread in all frequency bands. In general, apply this limit only if the number of measurement points, N, is greater than 10.

#### 3. EXAMPLE.

#### 3.1 Input Test Data Set.

Table 516.6A-II represents a homogeneous table of normally distributed numbers of unity variance around a mean value of 3.5 with N=14 rows and M=5 columns (rows could represent fourteen individual test measurements and columns could represent test values over five individual frequency bandwidths). Table 516.6A-II is used in the upper limit determinations in paragraphs 3.2 and 3.3 below.

3.0674	3.3636	2.0590	2.4435	3.8803
1.8344	3.6139	4.0711	4.9151	2.4909
3.6253	4.5668	3.1001	2.6949	3.4805
3.7877	3.5593	4.1900	4.0287	3.4518
2.3535	3.4044	4.3156	3.7195	3.5000
4.6909	2.6677	4.2119	2.5781	3.1821
4.6892	3.7902	4.7902	1.3293	4.5950
3.4624	2.1638	4.1686	3.4408	1.6260
3.8273	4.2143	4.6908	2.4894	3.9282
3.6746	5.1236	2.2975	4.1145	4.3956
3.3133	2.8082	3.4802	4.0077	4.2310
4.2258	4.3580	3.3433	5.1924	4.0779
2.9117	4.7540	1.8959	4.0913	3.5403
5.6832	1.9063	3.7573	2.8564	4.1771

## Table 516.6A-II. Input test data set.

## 3.2 Parametric Upper Limits.

The upper normal one-sided tolerance limit (NTL) is computed as 95/50 limit with 50 percent confidence that at least 95 percent of the values will lie below this limit for  $k_{N, \beta, \gamma} = 1.68$  from Table 516.6A-I. The upper normal prediction limit (NPL) is computed with a 95 confidence coefficient at the 95 percent point of the distribution where  $t_{N-1;\alpha} = t_{13;0.05} = 1.771$ . Figure 516.6A-1 displays the data, and Figure 516.6A-2 displays the two parametric upper limits.

Note: The degree of conservativeness in the normal prediction upper limit over the normal tolerance limit.



Figure 516.6A-1. Input test data set.



Figure 516.6A-2. Parametric and non-parametric upper limits.

## 3.3 Nonparametric Upper Limits.

The envelope limit (ENV) along with the upper distribution-free tolerance limit (DFL) for  $\beta$  proportion of the population set at 0.95 and  $\gamma$  confidence coefficient of 0.51 for N=14 samples is displayed in Figure 516.6A-2. This represents one curve with two interpretations. The 95 percent upper empirical tolerance limit (ETL) is also displayed on Figure 516.6A-2 where at least 95 percent of the values will be exceeded by this limit with 50 percent confidence. The data are displayed on Figure 516.6A-2 for comparison purposes.

## 3.4 Observations.

The "flatness" of the upper limits on Figure 516.6A-2 attests to the homogeneity of the data in Table 516.6A-II. It is apparent from Figure 516.6A-2 that the upper limits for the parameters selected are not "statistically equivalent." Of the two upper limit estimates, the NTL is favored if it can be established that the logarithm transform of the data set is approximately normally distributed. The closeness of the nonparametric envelopes attests also to the homogeneity of the data in Table 516.6A-II in addition to demonstrating, for this case at least, the nonstatistical ENV, the statistically based DFL and the ETL basically agree with regard to the upper limit magnitude. For nonhomgeneous data sets ETL would not be expected to agree with ENV or DFL. For small data sets, ETL may vary depending upon if "k" rounds upward or downward.

## 3.5 MATLAB m-function "ul."

Following is a MATLAB function "ul" for computing the specified upper limit and any associated parameters. The desired upper limit is input through str in with associated parameters in par in. The N by M matrix of data values is input in the N by M matrix X\_in. The output upper limit is in X\_ul with selected parameters computed within the function in par\_out. The following function has been verified with the data matrix supplied in Table 516.6A-II of this Annex. Before applying, the user must clearly understand the input and verify the m-function with a simple example. The input displayed in Table 516.6A-II was generated with the following MATLAB command:

 $X_{in} = randn(14,5) + 3.5;$ 

function [par_out,X_ul] = ul(str_in,par_in,X_in)	
* ul.m - MATIAB m-function for determining a data array upper limit 11-May-1999	<pre>for i = 1:M</pre>
a Maint Information :	end else
* * * str_in - input string specifying the desired upper limit and transform	X_UL = T + K_N_BECA_Gamma*S; end
* * par_in - input parameters for desired upper limit	end stystststststststststststststststature - Normal Prediction Limit \$ struture
<pre>% In - a N by M matrix of data values. N rows in X in representing individual measurement points. M columns in X in representing independently processed values. For a specified Togarithm transformation of X in, all the values in X in must be positive. For ETL the mean value for a column of X in ust not b zero.</pre>	<pre>in Str_In(1) == 'Nt'' t value = tinv(sar in(3), N_l);     t value = tinv(sar in(3), N_l);     for I = tinv     for I = 1:N         X_ul(i) = 10^(m(i) + s(i) * sgrt(1 + 1/N) * t_value);     end </pre>
<pre>% NTL % NTL % atr in(1:4) = 'NTLM'&gt; normal tolerance upper limit with log transform of X_in % atr_in(1:4) = 'NTLM'&gt; normal tolerance upper limit of X_in % par_in = [N K_N Beta Gauma]&gt; K_N Beta Gauma - one added normal % tolerance interval table value value with Beta portion and Gamma confidence</pre>	<pre>else x_ul = m + (sqrt(1 + 1/N) * t_value)*s; par_out(1)=t_value;</pre>
<pre>% NPL % NPL % str_in(1:4) = 'NPLM'&gt; normal prediction upper limit with log transform of X_in % str_in(1:4) = 'NPLM'&gt; normal prediction upper limit of X_in % part in = [N Gemma] -&gt;&gt; 0 &lt; Gemma [-1:4]pla) &lt; 1 - confidence coefficient * normal (1) = formal&gt;&gt; 0 &lt; Gemma [-1:4]pla) &lt; 1 - confidence coefficient</pre>	ento ento esta esta esta esta esta envolutor de la companya esta esta esta esta esta esta esta est
<pre>% Dot</pre>	83838383888888888888888888 DFL - Distribution Free Limit 88888888888888888888888888888888888
<pre>% DFL % Truin(1:4) = 'DFLN'&gt; distribution free upper limit % strin = [N M B G]&gt; for B = 0 or Beta - portion of population % par_in = [N M B G]&gt; for G = Gamma or 0 - confidence coefficient % par_in(1) = Beta - if par_in(3) = Beta and par in(4) = Gamma and par in(4) = 0</pre>	$\begin{array}{llllllllllllllllllllllllllllllllllll$
<pre>% ETL # ETL = * ETLM'&gt; empirical tolerance upper limit % atr in(1:4) = 'ETLM'&gt; empirical tolerance upper limit % par_in = [N Beta]&gt; 0 &lt; Beta &lt; 1 where Beta = portion of population % par_out(1) = u_Beta&gt; ordered value corresponding to Beta</pre>	<pre>par_out(1) = beta; endif par_out(1) &gt; 0 X_ul = nanmax(X_in); else</pre>
& Internation :	STWT='improper Beta/Gamma input :: exit function u!' end end
<pre>% par out - output parameters (if any) % par out - output parameters (if any) % X_ul - a 1 by M data vector specifying the desired upper limit</pre>	8488888888888888888888888888888888888 15 str_in(1:3) == 'ETL' \$\$\$ normalize with respect to the column mean
<pre>% % % = par_in(1); if N &gt; 1</pre>	X=ZEFOS (L.NN); X o=ZEFOS (1,NN); FOT i = 1.N
$M^{-1} = M - 1;$ $M^{-1} = par in(2);$ $MM = M > M_{2}.$	ror J = 1:M X (j+(i-1)*N)=X_in(i,j)/m(j); end
par ou(1)=0; $x u = arcs(1, M);$ $x = x (x, x)$	end 8. order X V 5. order X
If Str In(4:4) = 'L' $X t = log10(X in)_{t}$	$ \frac{\Lambda}{10} \frac{0 = SOT(L(\Lambda))}{10 \text{ for } (1 \text{ for } 1)} \times NM $
$\frac{1}{X} t = X_{in}$	11 MM J= M_ILINGX > 0 Ul = X_O(Ul index)
\$\$\$ mean of N rows over M columns of $X_{L}$ m = mean (X t);	gar - uc(t) - ut, X uI = uI + n;
<pre>%%% standard deviation of N rows over M columns of X_t s = stof(1;); s = acon_ar on a v n;</pre>	erse STWT = 'improper Beta input :: exit function ul' end
par out (1) = 0; X ul-zeros(1,M); \$859\$\$8\$ NTL - Normal Tolerance Limit \$	end else STMT = 'N < 2 :: exit function ul'
$IL str_in(1:s) = str_in(3);$ $k N Beck damma = par_in(3);$ $if str_in(4:4) == T_i$	8 8 end of function ul

Figure 516.6A-3. MATLAB m-function "ul" for upper limit determination.

#### 4. RECOMMENDED PROCEDURES.

## 4.1 Recommended Statistical Procedures for Upper Limit Estimates.

Paragraph 6.1, reference b, provides a detailed discussion of the advantages and disadvantages of estimate upper limits. The guidelines in this reference will be recommended here. In all cases plot the data carefully with a clear indication of the method of establishing the upper limit and the assumptions behind the method used.

- a. When N is sufficiently large, i.e., N  $\geq$  7, establish the upper limit by using the expression for the DFL for a selected  $\beta \geq 0.90$  such that  $\gamma \geq 0.50$ .
- b. When N is not sufficiently large to meet the criterion in (a), establish the upper limit by using the expression for the NTL. Select  $\beta$  and  $\gamma \ge 0.50$ . Variation in  $\beta$  will determine the degree of conservativeness of the upper limit.
- c. For N > 10 and a confidence coefficient of 0.50, the upper limit established on the basis of ETL is acceptable and may be substituted for the upper limit established by DFL or NTL. It is important when using ETL to examine and confirm the homogeneity of the estimates over the frequency bands.

#### 4.2 Uncertainty Factors.

Uncertainty factors may be added to the resulting upper limits if confidence in the data is low or the data set is small. Factors on the order of 3 dB to 6 dB may be added. Paragraph 6.1, reference b recommends a 5.8 dB uncertainty factor (based on "flight-to-flight" uncertainties of 3 dB, and "point-to-point" uncertainties of 5 dB) be used with captive carry flight measured data to determine a maximum expected environment using a normal tolerance limit. It is important that all uncertainties be clearly defined and that uncertainties are not superimposed upon estimates that already account for uncertainty.

## **METHOD 516.6 ANNEX B**

## **Effective Shock Duration**

#### 1. SCOPE.

#### 1.1 Purpose.

This Annex provides a basis and justification for the selection of the definition of an effective shock duration, Te.

#### 1.2 Application.

Information in this Annex is directed towards selection of an effective shock duration for laboratory testing based upon measured data. Replication of field measured environments in the laboratory by use of synthesized complex transients on exciter control systems requires (1) satisfaction of the field measured SRS amplitude and (2) correspondence between the duration of the field measured transient and the laboratory synthesized transient. In certain cases it may be apparent that one amplitude-varying shock over a long duration may actually be two or more distinct shocks over the duration. The requirements for deciding if field measured data should be replicated in the laboratory as a single shock or as multiple shocks are (1) a clear understanding of the physical phenomenon behind the field measured environment along with an understanding of the frequency characteristics of the test item, and (2) the judgment of an experienced analyst.

#### 2. DEVELOPMENT.

#### 2.1 Assumptions on Shock Envelope Development.

The shock duration is essentially determined by the form of the envelope of the absolute value of the measured peaks of the shock time history. This tacitly assumes that for a shock time history, the distribution of the positive and negative peaks of the shock time history are essentially the same, i.e., the shock time history is symmetrical with respect to polarity. The envelope of these peaks, in general, is a complex piecewise continuous function that has no simple analytical description. Figure 516.6B-1A displays a typical shock time history along with its envelope and two sets of vertical lines – one indicating the duration of  $T_E$  and the other the duration of  $T_e$ . Figure 516.6B-1B displays short time average RMS, along with one set of vertical lines indicating the duration of  $T_e$ . In the development to follow, it is assumed that the measured shock transient peak distribution in time has an initial segment characterized by a rise time ( $t_r$ ), and a following segment characterized by a decay time ( $t_d$ ) where, in general,  $t_d > t_r$ . It is assumed that the envelope of the initial peak amplitude distribution normalized to the absolute value of the maximum peak acceleration, Ap, is of a third order polynomial form

$$e_r(t) = a_1\left(\frac{t}{t_r}\right) + a_2\left(\frac{t}{t_r}\right)^2 + a_3\left(\frac{t}{t_r}\right)^3$$
  $0 \le t \le t_r \text{ and } a_1 + a_2 + a_3 = 1$ 

It is also assumed that the envelope of the trailing segment is characterized by a simple exponentially decaying function normalized to Ap

$$e_{j}(t) = e^{\alpha \left(\frac{t}{t_{r}}-1\right)} \qquad \qquad t_{r} \leq t \leq t_{r}+t_{j}$$

The initial segment has three degrees of freedom for fitting, whereas the trailing segment has one degree of freedom. The segments will, in general, have a much more complex form than can be represented by the simple expressions  $e_r(t)$  and  $e_j(t)$ . In general, the SRS amplitudes in the high frequency region are more sensitive to the initial segment form than the trailing segment form, whereas the low frequency SRS amplitudes are sensitive to both the duration of the trailing segment and to the form of the trailing segment.



Figure 516.6B-1a. Typical shock time history with envelope,  $T_E$  and  $T_e$ .



Figure 516.6B-1b. Typical shock time history RMS with envelope and Te.

## 2.2 $T_e$ versus $T_E$ .

 $T_E$  was defined in MIL-STD-810E to be "the minimum length of time that contains all data magnitudes exceeding 1/3 of the peak magnitude associated with the shock event." In MIL-STD-810F as well as in this document,  $T_e$  is defined to be the minimum length of time that contains at least 90 percent of the root-mean-square (RMS) time history amplitudes exceeding in value 10 percent of the peak RMS magnitude associated with the shock event. Figure 516.6B-2 provides a scatter plot of  $T_E$  versus  $T_e$  for shocks simulated according to the envelope forms above, and provides a visual correlation between the two durations. From this statistical simulation, on this particular

simple form of pulse, it can be concluded that the median ratio of  $T_e$  to  $T_E$  is 2.62 with 95 percent of the ratios lying between 1.71 and 5.43.



Figure 516.6B-2. Scatter plot T<sub>E</sub> versus T<sub>e</sub>

**NOTE**: Median Ratio  $T_e/T_E$  2.62 with 95 percent of Ratios between 1.71 and 5.43.

## 3. RECOMMENDED PROCEDURES FOR SYNTHESIS AND ANALYSIS.

## 3.1 Synthesis Recommended for T<sub>e</sub>.

Table 516.6-I contains the recommended values of  $T_e$  replacing the  $T_E$  values in editions of MIL-STD-810 prior to MIL-STD-810F. Use these values of  $T_e$  for guidance in specifying the duration of a synthesized complex transient for laboratory testing. In general,  $T_e$  may be considered to be approximately 2.5  $T_E$ .

 Table 516.6B-I (Same as Table 516.6-I).
 Test shock response spectra for use if measured data are not available.

Test Category	Peak Acceleration (g's)	T <sub>e</sub> (ms)	Cross-over Frequency (Hz)
Functional Test for Flight Equipment	20	15-23	45
Functional Test for Ground Equipment	40	15-23	45
Crash Hazard Shock Test for Flight Equipment	40	15-23	45
Crash Hazard ShockTest for Ground Equipment	75	8-13	80

Note 1: Refer to guidance in paragraph 2.3.3 c and d to customize the bandwidth of the SRS and  $T_e$ .

## 3.2 Synthesis Uncertainty Factors for T<sub>e</sub>.

Table 516.6B-I contains the uncertainty factors in the effective duration,  $T_e$ . Use these uncertainty factors for  $T_e$  for guidance in specifying the duration of a synthesized complex transient for laboratory testing.

## 3.3 Analysis Relationship to T<sub>e</sub>.

For computation of the SRS of the shock event (for durations in which  $T_e > \frac{1}{2f_{min}}$  where  $f_{min}$  is the minimum SRS

frequency of interest), taper the beginning and the end of the shock event to zero amplitude, and extend the time of the computation over the tapers and the duration  $T_e$ . Computation of the ESD or FT of the shock event must have a minimum block size of length equivalent to the duration,  $T_e$ , and be zero padded to eliminate excess noise in the estimates based upon the judgment of an experienced analyst.

## METHOD 516.6 ANNEX C

## Autospectral Density with Equivalent Test Shock Response Spectra

#### 1. SCOPE.

#### 1.1 Purpose.

This Annex provides information for determination if a field measured or predicted stationary random vibration ASD provides an environment that exceeds that for a field measured or predicted shock.

#### 1.2 Application.

For field measured or predicted ASD data from high level stationary random vibration, if the data representative time history is such that it exceeds substantially the measured or predicted shock environment time history, the random vibration test may be considered to provide an adequate test for the shock environment. Perform only the stationary random vibration test.

#### 2. DEVELOPMENT.

#### 2.1 Assumptions on Autospectral Density.

Figure 516.6C-1 provides two ASD plots for functional tests for ground materiel and flight materiel. Figures 516.6C-2a and 516.6C-2b provide the associated simulated Gaussian stationary amplitude time history segments over a 25 ms period of time for the ground materiel and the flight materiel, respectively.



## Figure 516.6C-1 (Same as Figure 516.6-9). Random test input ASD yielding equivalent test SRS spectrum shown on Figure 516.6C-4 (Same as Figure 516.6-8) (for Procedure I - Functional Shock).



Figure 516.6C-2a Sample Gaussian time history for functional test for ground materiel.



Figure 516.6C-2b. Sample Gaussian time history for functional test for flight materiel.

## 2.2 Assumptions on Shock Response Spectra.

Figures 516.6C-3a and 516.6C-3b provide the associated SRS plots for 250 simulations of the time histories on Figure 516.6C-2a and 516.6C-2b, respectively. In particular, the SRS plots represent the mean SRS and the upper and lower distribution free tolerance intervals based upon a 98 percent proportion of population with a 92 percent confidence coefficient and the SRS spectra specified on Figure 516.6C-4. The SRS were computed for a Q=5 over approximately one second time interval, i.e., 10 times the period of the lowest frequency represented on Figure 516.6C-1.



Figure 516.6C-3a. SRS comparison for functional test for ground materiel.



Figure 516.6C-3b. SRS comparison for functional test for flight materiel.



Figure 516.6C-4 (Same as Figure 516.6-8). Test SRS for use if measured data are not available (for Procedure I - Functional Shock, & Procedure V - Crash Hazard Shock Test).

## 3. RECOMMENDED PROCEDURES.

## 3.1 Recommended for ASD.

For measured stationary random vibration data, compute the ASD and compare with the ASD of Figure 516.6C-1. If the measured ASD exceeds the ASD in this figure at every frequency with a maximum 5 Hz analysis filter bandwidth, perform only the random vibration test on the equipment.

## 3.2 Recommended for SRS.

For measured stationary random vibration data compute the ASD and compare with the ASD of Figure 516.6C-1. If the measured ASD does not exceed the ASD on this figure at every frequency with a maximum 5 Hz analysis filter bandwidth, sample the measured random vibration data and proceed to compute an SRS over a selected period of time no shorter than 10 times the period of the lowest frequency represented on Figure 516.6C-1. If the SRS exceeds the SRS of Figure 516.6C-4 at every frequency, consider the random vibration test adequate. If the SRS does not exceed the SRS of Figure 516.6C-4 at every frequency, proceed to generate a complex transient from either field measured or predicted SRS data in order to test the equipment for shock.